



# 4. Test Generation from Finite State Models III

## Model-Based Testing

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# The $\mathcal{W}$ -Method

Given an FSM  $\mathcal{M} = \langle \mathcal{X}, \mathcal{Y}, \mathcal{Q}, q_0, \delta, \mathcal{O} \rangle$  the  $\mathcal{W}$ -method consists of the following steps:

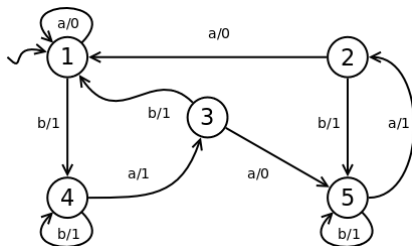
- 1 Estimate the maximum number of states in the correct design
- 2 Construct the characterization set  $\mathcal{W}$  for the given machine  $\mathcal{M}$
- 3 Construct the testing tree for  $\mathcal{M}$  and determine the **transition cover set**  $\mathcal{P}$
- 4 Construct set  $\mathcal{L}$
- 5  $\mathcal{P} \cdot \mathcal{L}$  is the desired test set

# $\mathcal{W}$ -method fault detection rationale

- A test case generated by the  $\mathcal{W}$  – method is of the form  $r \cdot s$  where  $r \in \mathcal{P}$  and  $s \in \mathcal{W}$ 
  - Why can we detect operation errors?
  - Why can we detect transfer errors?

$\mathcal{P} = \{\epsilon, a, b, bb, ba, bab, baa, baab, baaa, baaab, baaaa\}$

$\mathcal{W} = \{a, aa, aaa, baaa\}$

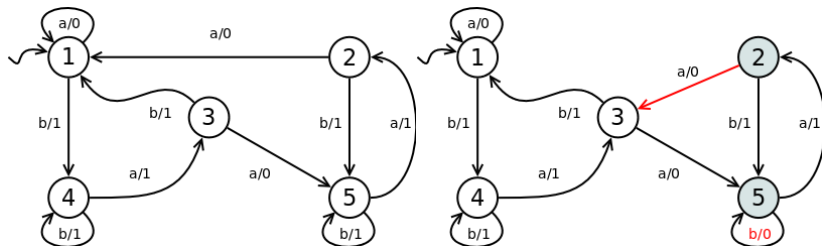


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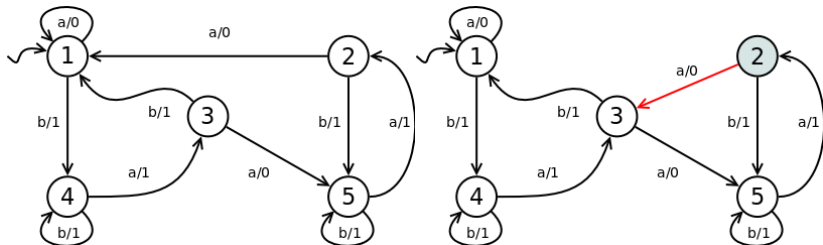


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# The partial $\mathcal{W}$ – method (aka $Wp$ – method)

$Wp$  – method main characteristics:

- is inspired by the  $\mathcal{W}$  – method it generates **smaller test sets**
- uses a derivation phase split in two phases that make use of **state identification sets**  $\mathcal{W}_i$  instead of characterization set  $\mathcal{W}$
- uses the **state cover set** ( $\mathcal{S}$ ) to derive the test set.
  - The state cover set is a nonempty set of sequences where each sequence belongs to  $\mathcal{X}^*$  and  $\forall q_i \in \mathcal{Q} \exists r \in \mathcal{S} \text{ s.t. } \delta(q_0, r) = q_i$
  - from the definition it is evident that  $\mathcal{S} \subseteq \mathcal{P}$

## The $\mathcal{W}p$ procedure (assuming $m = n$ )

The test set derived using the  $\mathcal{W}p$  – *method* is given by the union to two test sets  $\mathcal{T}_1, \mathcal{T}_2$  calculated according to the following procedure:

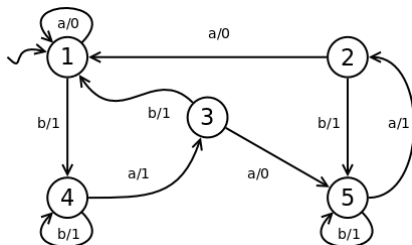
- 1 Compute sets  $\mathcal{P}, \mathcal{S}, \mathcal{W}$ , and  $\mathcal{W}_i$
- 2  $\mathcal{T}_1 = \mathcal{S} \cdot \mathcal{W}$
- 3 Let  $\mathcal{W} = \{\mathcal{W}_1, \mathcal{W}_2, \dots, \mathcal{W}_n\}$
- 4 Let  $\mathcal{R} = \{r_1, r_2, \dots, r_k\}$  where  $\mathcal{R} = \mathcal{P} - \mathcal{S}$  and  $r_j \in \mathcal{R}$  is s.t.  $\delta(q_0, r_j) = q_{ij}$
- 5  $\mathcal{T}_2 = \mathcal{R} \otimes \mathcal{W} = \cup_{j=1}^K (\{r_j\} \cdot \mathcal{W}_{ij})$  where  $\mathcal{W}_{ij} \in \mathcal{W}$  is the state identification set for state  $q_{ij}$

## $\mathcal{W}p$ – method rationale

- **Phase 1:** test are of the form  $uv$  where  $u \in \mathcal{S}$  and  $v \in \mathcal{W}$ . Reach each state than check if it is distinguishable from another one
- **Phase 2:** test covers all the missing transitions and then check if the reached state is different from the one specified in the model



## $\mathcal{W}$ p – method in practice



$$\mathcal{W} = \{a, aa, aaa, baaa\}$$

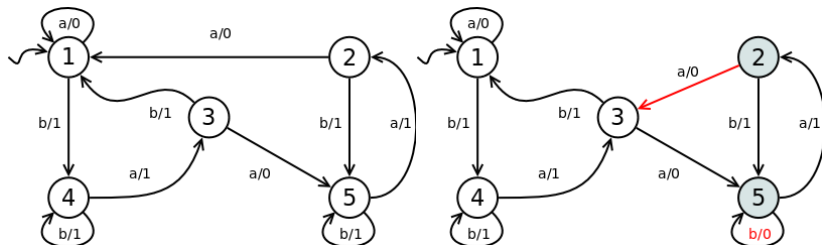
$$\mathcal{P} = \{\epsilon, a, b, bb, ba, bab, baa, baab, baaa, baaab, baaaa\}$$

$$\mathcal{S} = \{\epsilon, b, ba, baa, baaa\}$$

$$\mathcal{W}_1 = \{baaa, aa, a\}, \mathcal{W}_2 = \{baaa, aa, a\}, \mathcal{W}_3 = \{aa, a\}$$

$$\mathcal{W}_4 = \{aaa, a\}, \mathcal{W}_5 = \{aaa, a\}$$

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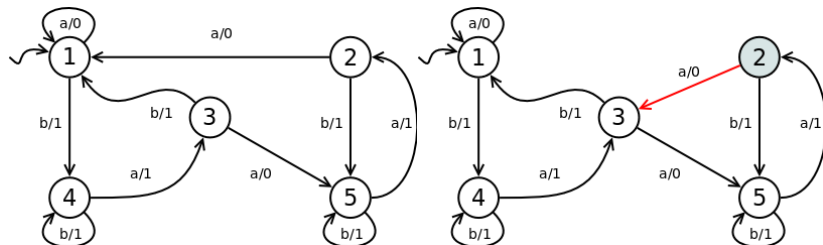
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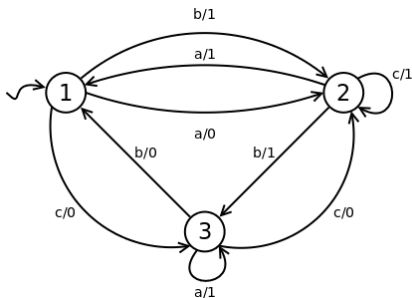
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# Is it phase 2 needed?

Let's consider the following FSM:



Now introduce an operation error or a transfer error on a “c” transition

## The $\mathcal{W}p$ procedure (assuming $m > n$ )

Modify the derivation of the two sets as follows:

- $\mathcal{T}_1 = \mathcal{S} \cdot \mathcal{Z}$  where  $\mathcal{Z} = \mathcal{X}[m - n] \cdot \mathcal{W}$
- $\mathcal{T}_2 = \mathcal{R} \cdot \mathcal{X}[m - n] \otimes \mathcal{W} = \cup_{j=1}^K (\{r_{ij}\} \cdot \cup_{u \in \mathcal{X}[m-n]} u \cdot \mathcal{W}_1)$

Applying

# Assessment of automata theoretic strategies

Control Flow based techniques are typically assessed according to different criteria:

- State coverage
- Transition coverage
- Switch coverage (n-switch coverage)
- Boundary-interior coverage