# 5. Generation from Combinatorial Design 

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## Combinatorial Design

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- Input space: all possible values that can be taken by input variables

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- factors: parameters possibly influencing program behaviour
- levels: values that can be assumed by a factor


## Combinatorial test-design process



Each factor combination may lead to one or more test cases where each test case consists of values of input variables and the expected output. Nevertheless, as usual the generation of all combinations is generally not feasible

## Fault model

The approach we are going to discuss targets interaction faults

- interaction faults are triggered when a certain combination of $t \geq 1$ parameter values causes the program containing the fault to enter an invalid state
- faults triggered by some value of input variables regardless of the values of other inputs variables are known as simple faults. When $t=2$ they are known as pairwise interaction faults. For arbitrary value of $t$ we refer to $t$-way interaction faults.


## Example - 1

Imagine a program that should return the value calculated by different combinations of a couple of functions. In particular when $x=x 2$ and $y=y 2$ the returned value should be $f(x, y, z)+g(x, y)$. Now consider the program:

```
begin
    int x,y,z;
    input (x,y,z);
    if (x==x1 and y==y2)
        output(f(x,y,z));
    else
        if (x==x2 and y==y1)
            output(g(x,y));
        else
            output(f(x,y,z)+g(x,y));
end
```


## Example - 2

Let $x, y \in\{-1,0,1\}$ and $z \in\{0,1\}$. Are there interaction faults that can be discovered in the following code snippet?

```
begin
    int x,y,z,p;
    input (x,y,z);
    p = (x+y)*z; // instead should be (x-y)*z
    if (p >= 0)
        output(f(x,y.z));
    else
    output (g(x,y));
end
```


## Fault vectors and Latin squares

- A fault vector is a k-uple of values for the factors of a program able to trigger a fault. The vector is considered a $t$-fault vector if any $t \leq k$ elements in V are needed to trigger the fault in P .
- A Latin Square of order $n$ is an $n \times n$ matrix such that no symbol appears more than once in a row and a column where the alphabet set $\Sigma$ as cardinality $n$.
e.g. $\Sigma=\{A, B\}$ and $\Sigma=\{1,2,3\}$


## Latin squares properties

Given a Latin square described by matrix $\mathscr{M}$ a large number of same order matrices can be obtained through row and column interchange and symbol-renaming operations.
A latin square obtained by the mentioned operations is said to be isomorphic to the starting latin square

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## Mutually orthogonal latin squares (MOLS)

MOLS are a useful tool to generate $t$ - wise vectors from latin squares.
Two latin squares are mutually orthogonal if their combination in a matrix of the same order does not generate duplicates.
$\operatorname{MOLS}(n)$ indicates a set of MOLS of order n . If $n$ is prime MOLS(n) contains $n-1$ MOLS and it is referred as a complete set. MOLS exists for each $n>2 \wedge n \neq 6$

Let's build the MOLS(5) set

## Pairwise design - binary factors

Now le's consider tree factors $X, Y, Z$ each one with two levels, and let's generate a pairwise design.

Generalizing the problem on $n$ factors each one having two levels.

- we need to define $\mathscr{S}_{2 k-1}$ to be the set of strings of lenght $2 k-1$ such that each string has exactly $k$ 1s. e.g. $k=3$

|  | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 1 | 1 | 1 |
| 2 | 0 | 1 | 1 | 1 | 0 |
| 3 | 1 | 1 | 1 | 0 | 0 |
| 4 | 1 | 0 | 1 | 1 | 1 |
| 5 | 0 | 1 | 1 | 0 | 1 |
| 6 | 1 | 1 | 0 | 1 | 0 |
| 7 | 1 | 0 | 1 | 0 | 1 |
| 8 | 0 | 1 | 0 | 1 | 1 |
| 9 | 1 | 1 | 0 | 0 | 1 |
| 10 | 1 | 0 | 0 | 1 | 1 |

## The SAMNA procedure

Input: n - number of two-valued input variables (factors) Output: A set of factor combinations such that all pairs of input values are covered
(1) Compute the smallest integer $k$ such that $n \leq\left|\mathscr{S}_{2 k-1}\right|$
(2) Select any subset of $n$ strings from $\mathscr{S}_{2 k-1}$. Arrange these to form an $n \times(2 k-1)$ matrix with one string in each row, while the columns contain different bits each string
(3) Append a columns of 0 s to the end of each string selected
(4) Each one of the $2 k$ columns contain a bit pattern from which we generate a combination is of the kind $\left(X_{1}^{*}, X_{2}^{*}, \ldots, X_{n}^{*}\right)$ where the value of each variable is selected depending on whether the bit in column $i, i \leq i \leq n$ is a 0 or a 1

## Example

Consider a simple Java applet named ChemFun that allows a user to create an in-memory database of chemical elements and search for an element.

| Factor | Name | Levels | Comments |
| :--- | :--- | :--- | :--- |
| 1 | Operation | \{Create,Show\} | Two buttons |
| 2 | Name | \{Empty,Nonempty\} | Data Field, String |
| 3 | Symbol | \{Empty,Nonempty\} | Data Field, String |
| 4 | Atomic Number | \{Invalid, Valid\} | Data Field, data $>0$ |
| 5 | Properties | \{Empty,Nonempty\} | Data Field, String |

Testing for all combinations would require a total of $2^{5}$ tests, but if we are interested for testing for pairwise interactions we can reduce the number of tests to 6 .

