

# Domain Specific Formal Languages

## CCS

Francesco Tiezzi

University of Camerino  
francesco.tiezzi@unicam.it

A.A. 2016/2017



# CCS Basics

## Sequential Fragment

- *Nil* process (the only atomic process)
- action prefixing ( $a.P$ )
- names and recursive definitions ( $\triangleq$ )
- nondeterministic choice ( $+$ )

Any finite LTS can be described (up to isomorphism) by using the operations above

## Parallelism and Renaming

- parallel composition ( $\parallel$ ) (synchronous communication between two components = handshake synchronization)
- restriction ( $P \setminus L$ )
- relabelling ( $P[f]$ )

# CCS Basics

## Sequential Fragment

- *Nil* process (the only atomic process)
- action prefixing ( $a.P$ )
- names and recursive definitions ( $\triangleq$ )
- nondeterministic choice ( $+$ )

Any finite LTS can be described (up to isomorphism) by using the operations above

## Parallelism and Renaming

- parallel composition ( $\parallel$ ) (synchronous communication between two components = handshake synchronization)
- restriction ( $P \setminus L$ )
- relabelling ( $P[f]$ )

# CCS Basics

## Sequential Fragment

- *Nil* process (the only atomic process)
- action prefixing ( $a.P$ )
- names and recursive definitions ( $\triangleq$ )
- nondeterministic choice ( $+$ )

Any finite LTS can be described (up to isomorphism) by using the operations above

## Parallelism and Renaming

- parallel composition ( $|$ ) (synchronous communication between two components = handshake synchronization)
- restriction ( $P \setminus L$ )
- relabelling ( $P[f]$ )

## Definition of CCS: channels, actions, process names

Let

- $\mathcal{A}$  be a set of **channel names** (e.g. *tea*, *coffee* are channel names)
- $\mathcal{L} = \mathcal{A} \cup \overline{\mathcal{A}}$  be a set of **labels** where
  - $\overline{\mathcal{A}} = \{\overline{a} \mid a \in \mathcal{A}\}$   
(elements of  $\mathcal{A}$  are called names and those of  $\overline{\mathcal{A}}$  are called co-names)
  - by convention  $\overline{\overline{a}} = a$
- $Act = \mathcal{L} \cup \{\tau\}$  is the set of **actions** where
  - $\tau$  is the **internal** or **silent** action  
(e.g.  $\tau$ , *tea*,  $\overline{\text{coffee}}$  are actions)
- $\mathcal{K}$  is a set of **process names (constants)** (e.g. CM).

## Definition of CCS (expressions)

$P := K$		process constants ( $K \in \mathcal{K}$ )
$\alpha.P$		prefixing ( $\alpha \in Act$ )
$\sum_{i \in I} P_i$		summation ( $I$ is an arbitrary index set)
$P_1   P_2$		parallel composition
$P \setminus L$		restriction ( $L \subseteq \mathcal{A}$ )
$P[f]$		relabelling ( $f : Act \rightarrow Act$ ) such that
		<ul style="list-style-type: none"><li>• <math>f(\tau) = \tau</math></li><li>• <math>f(\bar{a}) = \overline{f(a)}</math></li></ul>

The set of all terms generated by the abstract syntax is the set of **CCS process expressions** (and is denoted by  $\mathcal{P}$ )

### Notation

$$P_1 + P_2 = \sum_{i \in \{1,2\}} P_i$$

$$Nil = \sum_{i \in \emptyset} P_i$$

# Precedence

## Precedence

- 1 restriction and relabelling (tightest binding)
- 2 action prefixing
- 3 parallel composition
- 4 summation

Example:  $R + a.P | b.Q \setminus L$  means  $R + ((a.P) | (b.(Q \setminus L)))$

## Definition of CCS (defining equations)

### CCS program

A collection of **defining equations** of the form

$$K \triangleq P$$

where  $K \in \mathcal{K}$  is a process constant and  $P \in \mathcal{P}$  is a CCS process expression.

- Only one defining equation per process constant.
- Recursion is allowed: e.g.  $A \triangleq \bar{a}.A \mid A$ .



# Structural Operational Semantics for CCS

Structural Operational Semantics (SOS)—G. Plotkin 1981

Small-step operational semantics where the behaviour of a system is inferred using syntax driven rules

Given a collection of CCS defining equations, we define the following LTS  $(Proc, Act, \{\xrightarrow{a} \mid a \in Act\})$ :

- $Proc = \mathcal{P}$  (the set of all CCS process expressions)
- $Act = \mathcal{L} \cup \{\tau\}$  (the set of all CCS actions including  $\tau$ )
- transition relation is given by **SOS rules** of the form:

$$\text{RULE } \frac{\textit{premises}}{\textit{conclusion}} \quad \textit{conditions}$$

# SOS rules for CCS

( $\alpha \in Act$ ,  $a \in \mathcal{L}$ )

$$\text{ACT} \quad \frac{}{\alpha.P \xrightarrow{\alpha} P}$$

$$\text{SUM}_j \quad \frac{P_j \xrightarrow{\alpha} P'_j}{\sum_{i \in I} P_i \xrightarrow{\alpha} P'_j} \quad j \in I$$

$$\text{COM1} \quad \frac{P \xrightarrow{\alpha} P'}{P|Q \xrightarrow{\alpha} P'|Q}$$

$$\text{COM2} \quad \frac{Q \xrightarrow{\alpha} Q'}{P|Q \xrightarrow{\alpha} P|Q'}$$

$$\text{COM3} \quad \frac{P \xrightarrow{a} P' \quad Q \xrightarrow{\bar{a}} Q'}{P|Q \xrightarrow{\tau} P'|Q'}$$

$$\text{RES} \quad \frac{P \xrightarrow{\alpha} P'}{P \setminus L \xrightarrow{\alpha} P' \setminus L} \quad \alpha, \bar{\alpha} \notin L$$

$$\text{REL} \quad \frac{P \xrightarrow{\alpha} P'}{P[f] \xrightarrow{f(\alpha)} P'[f]}$$

$$\text{CON} \quad \frac{P \xrightarrow{\alpha} P'}{K \xrightarrow{\alpha} P'} \quad K \triangleq P$$

## Deriving Transitions in CCS

Let  $A \triangleq a.A$ . Then

$$((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a].$$

Why?

## Deriving Transitions in CCS

Let  $A \triangleq a.A$ . Then

$$((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a].$$

Why?

$$\text{REL} \frac{}{((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a]}$$

## Deriving Transitions in CCS

Let  $A \triangleq a.A$ . Then

$$((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a].$$

Why?

$$\text{REL} \frac{\text{COM1} \frac{}{(A \mid \bar{a}.Nil) \mid b.Nil \xrightarrow{a} (A \mid \bar{a}.Nil) \mid b.Nil}}{}{((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a]}}$$

## Deriving Transitions in CCS

Let  $A \triangleq a.A$ . Then

$$((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a].$$

Why?

$$\text{REL} \frac{\text{COM1} \frac{\text{COM1} \frac{A \mid \bar{a}.Nil \xrightarrow{a} A \mid \bar{a}.Nil}{(A \mid \bar{a}.Nil) \mid b.Nil \xrightarrow{a} (A \mid \bar{a}.Nil) \mid b.Nil}}{((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a]}}$$

## Deriving Transitions in CCS

Let  $A \triangleq a.A$ . Then

$$((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a].$$

Why?

$$\text{REL} \frac{\text{COM1} \frac{\text{COM1} \frac{\text{CON} \frac{A \triangleq a.A}{A \xrightarrow{a} A}}{A \mid \bar{a}.Nil \xrightarrow{a} A \mid \bar{a}.Nil}}{(A \mid \bar{a}.Nil) \mid b.Nil \xrightarrow{a} (A \mid \bar{a}.Nil) \mid b.Nil}}{((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a]}}$$

## Deriving Transitions in CCS

Let  $A \triangleq a.A$ . Then

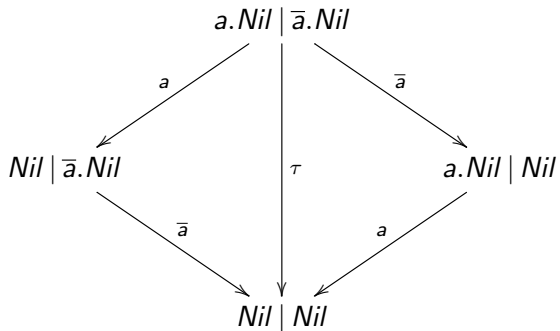
$$((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a].$$

Why?

$$\begin{array}{c} \text{ACT} \frac{}{a.A \xrightarrow{a} A} \\ \text{CON} \frac{a.A \xrightarrow{a} A}{A \xrightarrow{a} A} \quad A \triangleq a.A \\ \text{COM1} \frac{}{A \mid \bar{a}.Nil \xrightarrow{a} A \mid \bar{a}.Nil} \\ \text{COM1} \frac{}{(A \mid \bar{a}.Nil) \mid b.Nil \xrightarrow{a} (A \mid \bar{a}.Nil) \mid b.Nil} \\ \text{REL} \frac{}{((A \mid \bar{a}.Nil) \mid b.Nil)[c/a] \xrightarrow{c} ((A \mid \bar{a}.Nil) \mid b.Nil)[c/a]} \end{array}$$



# LTS of the Process $a.Nil \mid \bar{a}.Nil$



## CCS: vending machine example



Examples at the blackboard. . .