

# Ambiguity

A grammar that produces **more than one parse tree** for some sentence is said to be ambiguous. An ambiguous grammar has **more than one left-most derivation** or **more than one rightmost derivation** for the same sentence.

## Ambiguity and Precedence of Operators

Using the simplest grammar for expressions let's derive again the parse tree for:

**id + id \* id**

Now consider the following grammar:

$$E \rightarrow E + T \mid E - T \mid T$$

$$T \rightarrow T * F \mid T / F \mid F$$

$$F \rightarrow (E) \mid \text{id}$$

## Use of ambiguous grammar

In some case it can be convenient to use ambiguous grammar, but then it is necessary to define **precise disambiguating rules**

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## Conditional statements

Consider the following grammar:

$$\begin{aligned} stmt &\rightarrow \mathbf{if\ expr\ then\ stmt} \\ &| \mathbf{if\ expr\ then\ stmt\ else\ stmt} \\ &| \mathbf{other} \end{aligned}$$

decide if the following sentence belongs to the generated language:

**if  $E_1$  then if  $E_2$  then  $S_1$  else  $S_2$**

# Exercises

Consider the grammar:

$$S \rightarrow SS + \mid SS * \mid a$$

and the string  $aa + a*$

- ▶ Give the leftmost derivation for the string
- ▶ Give the rightmost derivation for the string
- ▶ Give a parse tree for the string
- ▶ Is the grammar ambiguous or unambiguous?
- ▶ Describe the language generated by this grammar?

Define grammars for the following languages:

- ▶  $\mathcal{L} = \{w \in \{0, 1\}^* \mid w \text{ is palindrom}\}$
- ▶  $\mathcal{L} = \{w \in \{0, 1\}^* \mid w \text{ contains the same occurrences of 0 and 1}\}$

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So what we can do?

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- ▶ Many languages admit both ambiguous and unambiguous grammars, while some languages admit only ambiguous grammars
- ▶ A language that only admits ambiguous grammars is called an inherently ambiguous language, e.g.  
 $\{a^n b^m c^k \mid n = m \text{ or } m = k; n, m, k \geq 0\}$
- ▶ A Turing machine cannot decide whether a context-free language is inherently ambiguous or not



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# ToC

- 1 Syntax Analysis: the problem
- 2 Theoretical Background
- 3 Syntax Analysis: solutions**
  - Top-Down parsing
  - Bottom-Up Parsing

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# Left Recursion

## Left recursive grammars

A grammar  $\mathcal{G}$  is **left recursive** if it has a non terminal  $A$  such that there is a derivation  $A \xRightarrow{*} A\alpha$  for some string  $\alpha$ . **Top-down parsing strategies cannot handle left-recursive grammars**

## Immediate left recursion

A grammar has an **immediate left recursion** if there is at least one production of the form  $A \rightarrow A\alpha$ . It is possible to transform the grammar still generating the same language and removing the left recursion. Consider the general case:

$$A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_m \mid \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$$

where  $n, m \geq 1$  and all  $\beta_i$  do not start with  $A$ . Equivalent productions are:

$$\begin{aligned} A &\rightarrow \beta_1 A' \mid \beta_2 A' \mid \dots \mid \beta_n A' \\ A' &\rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \dots \mid \alpha_m A' \mid \epsilon \end{aligned}$$

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