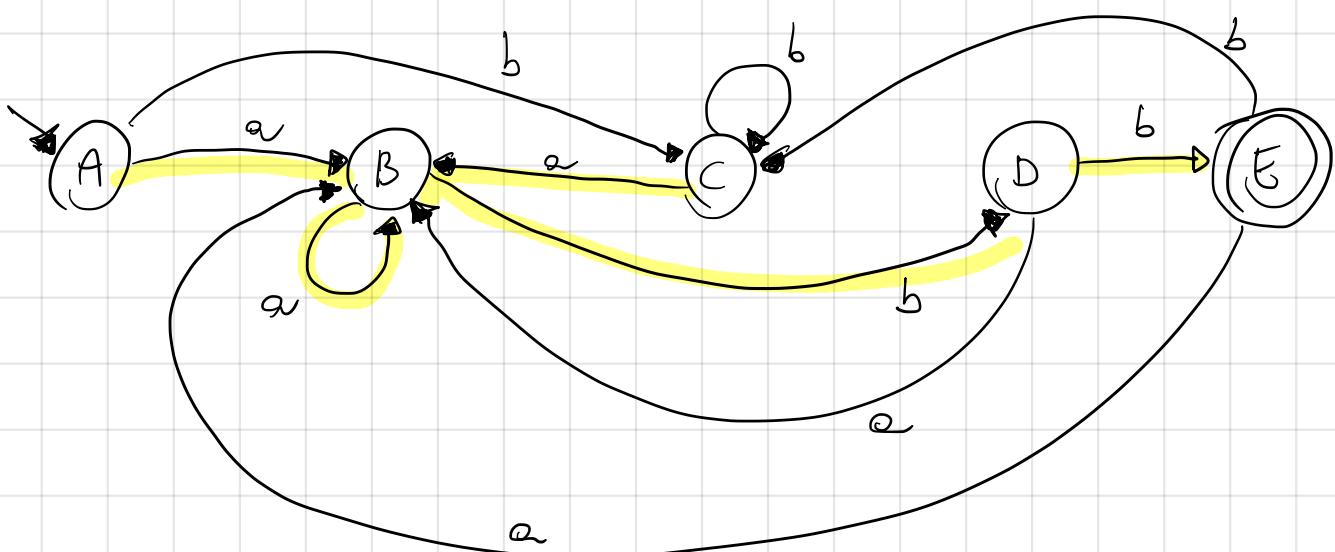
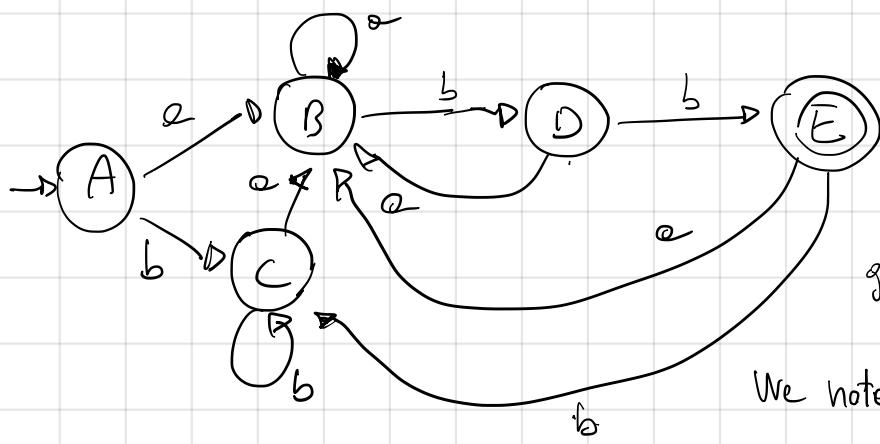


$\Sigma$	$\{a\}$	$b$
$\epsilon\text{-cl}(\{i\}) = \{i, 1, 2\}$ $\{4, 7\} = A$	$\epsilon\text{-closure}(move(\{i, 1, 2, 4, 7\}, a)) = \{5, 6, 7, 1, 2, 4, 8\}$ $= B$	$\dots \epsilon\text{-cl}(\{3\}) = \{3, 6, 7, 1, 2, 4\} = C$
$B = \{5, 6, 7, 1, 2, 4, 8\}$	$B$	$\epsilon\text{-cl}(\{3, 9\}) = \{3, 6, 7, 1, 2, 4, 9\} = D$
$C = \{3, 6, 7, 1, 2, 4\}$	$B$	$\epsilon\text{-cl}(\{3, f\}) = \{3, 6, 7, 1, 2, 4, f\} = E$
$E = \{3, 6, 7, 1, 2, 4, f\}$ $\in F_B$	$B$	$C$



$$ab \circ b \circ b \quad A \xrightarrow{a} B \xrightarrow{b} D \xrightarrow{a} B \xrightarrow{b} D \xrightarrow{b} E$$

If  $|N| = n$  then the powerset of  $N$ , denoted by  $2^N$  or  $\text{Pow}(N)$ , has  $2^n$  elements.



$$\Pi^{(1)} = \{\{E\}, \{A, B, C, D\}\}$$

We try to refine the group  $\{A, B, C, D\}$  into subgroups.

We note that  $D \xrightarrow{b} \{E\}$

$$\{A, B, C\} \xrightarrow{b} \{A, B, C, 0\}$$

Thus,  $D$  can be put outside the group:  $\Pi^{(2)} = \{\{E\}, \{D\}, \{A, B, C\}\}$

We note that  $B \xrightarrow{b} \{D\}$

$$\{A, C\} \xrightarrow{b} \{A, B, C\}$$

Thus  $\Pi^{(3)} = \{\{E\}, \{D\}, \{B\}, \{A, C\}\}$

Finally  $A \xrightarrow{a} \{B\}$   
 $C \xrightarrow{a} \{B\}$

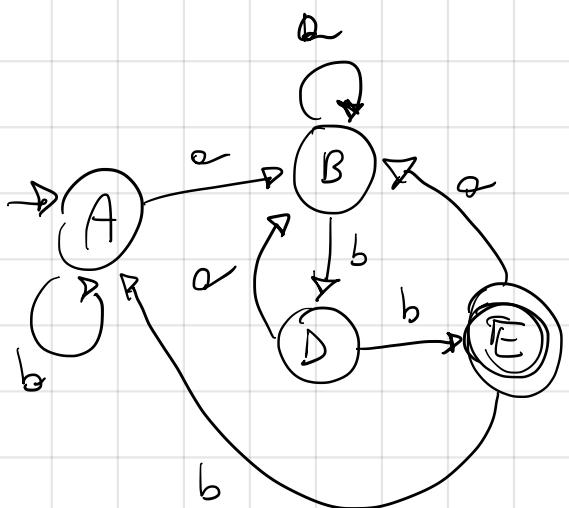
$$\begin{array}{l} A \xrightarrow{b} \{A, C\} \\ C \xrightarrow{b} \{A, C\} \end{array}$$

Thus,  $\{A, C\}$  cannot

be decomposed further.

This means that  $\Pi^{(4)} = \Pi^{(3)} = \{\{E\}, \{D\}, \{B\}, \{A, C\}\}$ ,

which is the finest partition possible. Let us draw the resulting minimal DFA by choosing  $A$  as the representative state of the group  $\{A, C\}$ :



Minimal DFA for

$$(a|b)^* ab^2$$