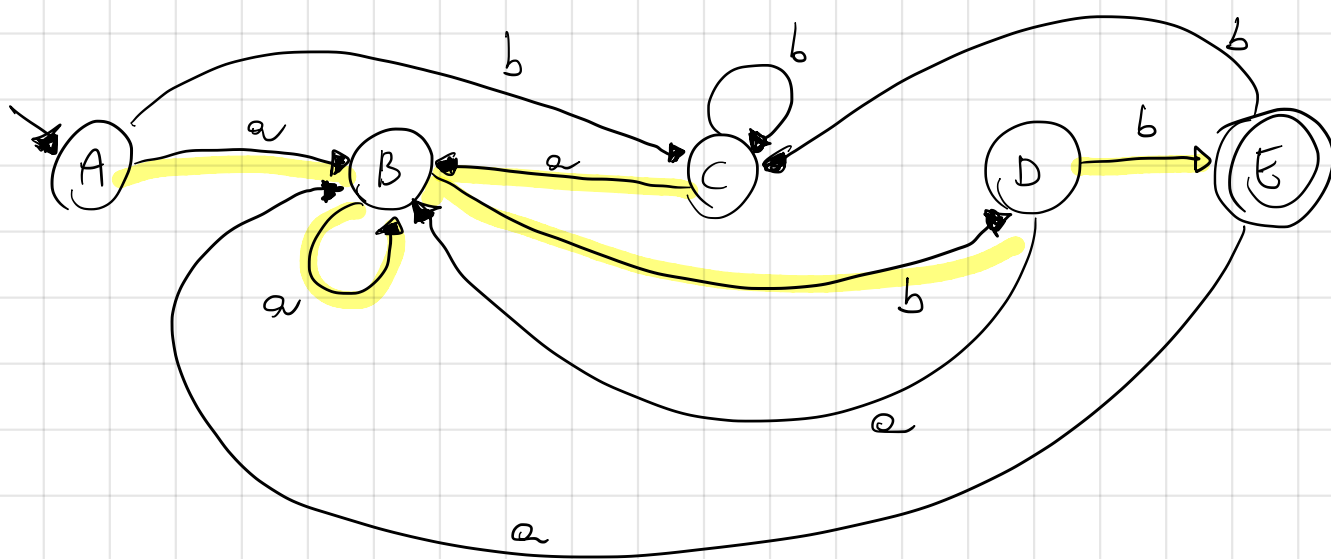
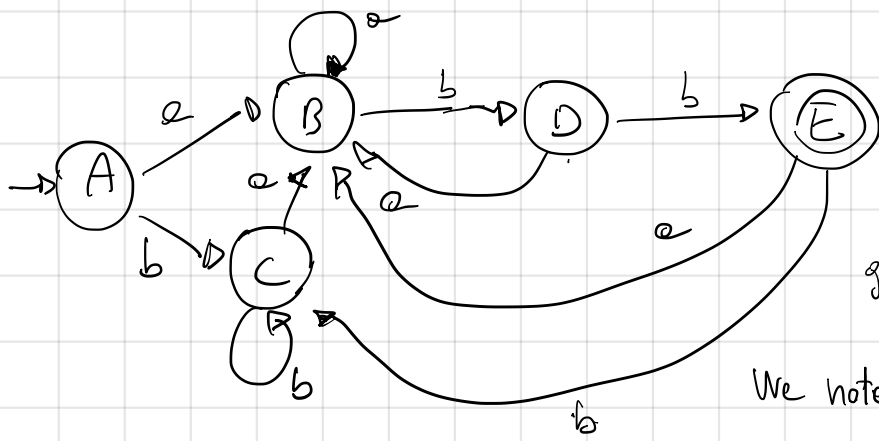


Σ	a	b
$\epsilon\text{-cl}_{\Sigma}(\{0\}) = \{0, 1, 2, 4, 7\} = A$	$\epsilon\text{-closure}(\text{move}(\{0, 1, 2, 4, 7\}, a)) = \epsilon\text{-cl}_{\Sigma}(\{5, 8\}) = \{5, 6, 7, 1, 2, 4, 8\} = B$	$\dots \epsilon\text{-cl}_{\Sigma}(\{3\}) = \{3, 6, 7, 1, 2, 4\} = C$
$B = \{5, 6, 7, 1, 2, 4, 8\}$	B	$\epsilon\text{-cl}_{\Sigma}(\{3, 9\}) = \{3, 6, 7, 1, 2, 4, 9\} = D$
$C = \{3, 6, 7, 1, 2, 4\}$	B	C
$D = \{3, 6, 7, 1, 2, 4, 9\}$	B	$\epsilon\text{-cl}_{\Sigma}(\{3, f\}) = \{3, 6, 7, 1, 2, 4, f\} = E$
$E = \{3, 6, 7, 1, 2, 4, f\} \in F_{\Sigma}$	B	C



$a b a b b$ $A \xrightarrow{a} B \xrightarrow{b} D \xrightarrow{a} B \xrightarrow{b} D \xrightarrow{b} E$

if $|N| = n$ then the powerset of N , denoted by 2^N or $\text{Pow}(N)$, has 2^n elements.



$$\Pi^{(1)} = \{\{E\}, \{A, B, C, D\}\}$$

We try to refine the group $\{A, B, C, D\}$ into subgroups.

We note that $D \xrightarrow{b} \{E\}$

$$\{A, B, C\} \xrightarrow{b} \{A, B, C, D\}$$

Thus, D can be put outside the group: $\Pi^{(2)} = \{\{E\}, \{D\}, \{A, B, C\}\}$

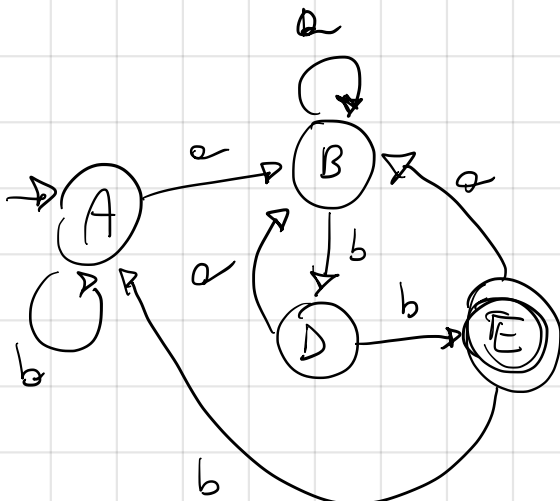
We note that $B \xrightarrow{a} \{D\}$

$$\{A, C\} \xrightarrow{a} \{A, B, C\} \quad \text{Thus } \Pi^{(3)} = \{\{E\}, \{D\}, \{B\}, \{A, C\}\}$$

Finally $A \xrightarrow{a} \{A, C\}$ $A \xrightarrow{b} \{A, C\}$ $C \xrightarrow{a} \{A, C\}$ $C \xrightarrow{b} \{A, C\}$ Thus, $\{A, C\}$ cannot be decoupled further.

This means that $\Pi^{(4)} = \Pi^{(3)} = \{\{E\}, \{D\}, \{B\}, \{A, C\}\}$,

which is the finest partition possible. Let us draw the resulting minimal DFA by choosing A as the representative state of the group $\{A, C\}$:



Minimal DFA for $(a|b)^*abb$