



2. Lexical Analysis

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ToC

1 Lexical Analysis: What does a Lexer do?

2 Short Notes on Formal Languages

Lexical Analysis

```
if (i==j)
    z=0;
else
    z=1;
```

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\tif (i==j)\n\t\tz=0;\n\telse\n\t\tz=1;
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Token, Pattern Lexeme

Token

A **token** is a pair consisting of a token name and an optional attribute value. The token names are the input symbols that the parser processes.

Pattern

A **pattern** is a description of the form that the lexemes of a token may take. In the case of a keyword as a token, the pattern is just the sequence of characters that form the keyword.

Lexeme

A **lexeme** is a sequence of characters in the source program that matches the pattern for a token and is identified by the lexical analyzer as an instance of that token.

Lexical Analysis

- Token Class (or Class)

- In English: *Noun, Verb, Adjective, Adverb, Article, ...*
- In a programming language: *Identifier, Keywords, “(”, “)”, Numbers, ...*

Lexical Analysis

- Token classes corresponds to sets of strings
- Identifier
 - strings of letter or digits starting with a letter
- Integer
 - a non-empty string of digits
- Keyword
 - "else", "if", "while", ...
- Whitespace
 - a non-empty sequence of blanks, newlines, and tabs

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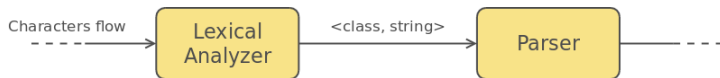
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Therefore the role of the lexical analyser (Lexer) is:

- Classify program substring according to role (token class)
- communicate tokens to parser

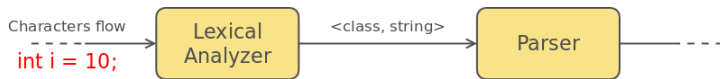


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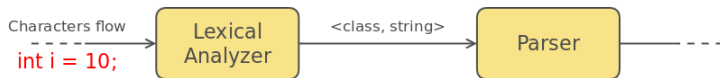


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Lexical Analysis

Let's analyse these lines of code:

```
\tif (i==j)\n\t\tz=0;\n\telse\n\t\tz=1;
```

```
x=0;\n\twhile (x<10) {\n\t\tx++;\n\t}
```

Token Classes: Identifier, Integer, Keyword, Whitespace

Lexical Analysis

Therefore an implementation of a lexical analyser must do two things:

- Recognise substrings corresponding to tokens
 - the lexemes
- Identify the token class for each lexemes

Lexical Analysis - Tricky problems

- FORTRAN rule: whitespace is insignificant
 - i.e. `VA R1` is the same as `VAR1`

```
DO 5 I = 1,25
```

```
DO 5 I = 1.25
```

In FORTRAN the "5" refers to a label you will find in the following of the program code

Lexical Analysis - Tricky problems

- The goal is to partition the string. This is implemented by reading left-to-right, recognising one token at a time
- “Lookahead” may be required to decide where one token ends and the next token begins
- PL/1 keywords are not reserved

```
IF ELSE THEN THEN = ELSE; ELSE ELSE = THEN
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```
DECLARE (ARG1, . . . , ARGN)
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Is DECLARE a keyword or an array reference?

Need for an unbounded lookahead

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Lexical Analysis - Tricky problems

- C++ template syntax:

```
Foo<Bar>
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- C++ stream syntax:

```
cin >> var;
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Foo<Bar<Barr>>
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Languages

Language

Let Σ be a set of characters generally referred to as the *alphabet*. A **language** over Σ is a set of strings of characters drawn from Σ

Alphabet = English character \implies Language = English sentences
 Alphabet = ASCII \implies Language = C programs

Given $\Sigma = \{a, b\}$ examples of simple languages are:

- $\mathcal{L}_1 = \{a, ab, aa\}$
- $\mathcal{L}_2 = \{b, ab, aabb\}$
- $\mathcal{L}_3 = \{s \mid s \text{ has an equal number of } a\text{'s and } b\text{'s}\}$
- ...

Grammar Definition

Grammar

A **Grammar** \mathcal{G} is a tuple $\langle \mathcal{V}_T, \mathcal{V}_N, \mathcal{S}, \mathcal{P} \rangle$ where:

- ▶ \mathcal{V}_T is a finite and non empty set of terminal symbols (alphabet)
- ▶ \mathcal{V}_N is a finite set of non-terminal symbols s.t. $\mathcal{V}_N \cap \mathcal{V}_T = \emptyset$
- ▶ $\mathcal{S} \in \mathcal{V}_N$ is the start symbol
- ▶ \mathcal{P} is a finite set of productions s.t. $\mathcal{P} \subseteq (\mathcal{V}^* \cdot \mathcal{V}_N \cdot \mathcal{V}^*) \times \mathcal{V}^*$ where $\mathcal{V}^* = \mathcal{V}_T \cup \mathcal{V}_N$

Derivations

Derivations

Given a grammar $\mathcal{G} = \langle \mathcal{V}_T, \mathcal{V}_N, \mathcal{S}, \mathcal{P} \rangle$ a derivation is a sequence of strings $\phi_1, \phi_2, \dots, \phi_n$ s.t.

$\forall i \in \{1, \dots, n\}. \phi_i \in \mathcal{V}^* \wedge \forall i \in \{1, \dots, n-1\}. \exists p \in \mathcal{P}: \phi_i \rightarrow^p \phi_{i+1}$

We generally write $\phi_1 \rightarrow^* \phi_n$ to indicate that from ϕ_1 it is possible to derive ϕ_n repeatedly applying productions in \mathcal{P}

Generated Language

The language generated by a grammar $\mathcal{G} = \langle \mathcal{V}_T, \mathcal{V}_N, \mathcal{S}, \mathcal{P} \rangle$ corresponds to: $\mathcal{L}(\mathcal{G}) = \{x \mid x \in \mathcal{V}_T^* \wedge \mathcal{S} \rightarrow^* x\}$

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Chomsky Hierarchy

A hierarchy of grammars can be defined imposing constraints on the structure of the productions in set \mathcal{P} ($\alpha, \beta, \gamma \in \mathcal{V}^*$, $a \in \mathcal{V}_T$, $A, B \in \mathcal{V}_N$):

T0. Unrestricted Grammars:

- Production Schema: *no constraints*
- Recognizing Automaton: **Turing Machines**

T1. Context Sensitive Grammars:

- Production Schema: $\alpha A \beta \rightarrow \alpha \gamma \beta$
- Recognizing Automaton: **Linear Bound Automaton (LBA)**

T2. Context-Free Grammars:

- Production Schema: $A \rightarrow \gamma$
- Recognizing Automaton: **Non-deterministic Push-down Automaton**

T3. Regular Grammars:

- Production Schema: $A \rightarrow a$ or $A \rightarrow aB$
- Recognizing Automaton: **Finite State Automaton**

Meaning function \mathcal{L}

Meaning Function

Once you defined a way to describe the strings in a language it is important to define a meaning function \mathcal{L} that maps syntax to semantics

▶ e.g. the case for numbers

- Why using a meaning function?
 - Makes clear what is syntax, what is semantics
 - Allows us to consider notation as a separate issue
 - Expressions and meanings are not 1 to 1

Warning

It should never happen that the same syntactical structure has more meanings

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