

# Fundamentals of Reactive Systems

## General Info & Introduction

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A.A. 2018/2019



## Who I am



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# Schedule

<b>Mon</b>	<b>Tue</b>	<b>Wed</b>	<b>Thu</b>	<b>Fri</b>
9-11		9-11		

# Contents

- Introductory concepts on reactive systems
- Preliminary mathematical concepts
- Semantics of regular expressions
- Semantics of the operators of the process algebras CCS, CSP and ACP
- Main behavioural equivalences, weak and strong
- (A hint to) Hennessy-Milner Logic and ACTL
- Software tools for the automatic verification of software-intensive systems modelled by means of process algebras: TAPAs . . . and Maude, muCRL2, etc.

## Teaching material

- Rocco De Nicola. *A gentle introduction to Process Algebras*. Notes obtained by the restructuring of two entries (Process Algebras - Behavioural Equivalences) of Encyclopedia of Parallel Computing, David A. Padua (Ed.). Springer 2011; pp. 120-127 and pp. 1624-1636
- Luca Aceto, Anna Ingolfsson, Kim Guldstrand Larsen and Jiri Srba. *Reactive Systems. Modelling, Specification and Verification*. Cambridge University Press, 2007. ISBN: 9780521875462. Additional material available at book's site: <http://rsbook.cs.aau.dk>
- Course's slides
- Lecture notes, papers and slides may be given by the teacher for studying and for exercises
- TAPAs documentation <http://rap.dsi.unifi.it/tapas/>
- Maude documentation <http://maude.cs.illinois.edu>
- mCRL2 documentation <http://www.mcrl2.org/>

# Final exam

- **Written test:**
  - on the exam date a written test takes place, it has a mixed structure: solution of exercises, and open/close answer questionnaire
  - during the course **in itinere tests** take place; in case they are evaluated positively, they replace the written test of the exam date
- Realisation of a **project** using a specification/verification software tool, or writing of a report, with a **presentation**

# The Hard Life of Programmers (and Students)



Questions?

# Reactive Systems

Multiple processes (or threads) working together to achieve a common goal

- A sequential program has a single thread of control
- A concurrent program has multiple threads of control allowing it to perform multiple computations in parallel and to control multiple external activities occurring at the same time

## Communication

The concurrent threads exchange information via

- **indirect communication**: the execution of concurrent processes proceeds on one or more processors all of which access a shared memory; care is required to deal with shared variables
- **direct communication**: concurrent processes are executed by running them on separate processors, threads communicate by exchanging messages



# Why Concurrent/Distributed Systems

- 1 **Performance:** To gain from multiprocessing hardware (parallelism)
- 2 **Distribution:** Some problems require a distributed solution, e.g. client-server systems on one machine and the database on a central server machine
- 3 **Ease of programming:** Some problems are more naturally solved by concurrent programs
- 4 **Increased application throughput:** an I/O call need only to block one thread
- 5 **Increased application responsiveness:** High priority threads for user requests
- 6 **More appropriate structure:** For programs which interact with the environment, control multiple activities and handle multiple events

## Do I need to check reactive systems?

### Programming them is error prone

- Soviet nuclear false alarm incident (1983)  
[fault in sw for missile detections]
- Therac-25 radiation overdose (1985-1987)  
[sw interlock fault due to a race condition]
- MIM-104 Patriot Missile Clock Drift (1991)  
[a sw fault in the system's clock]
- Explosion of the Ariane 5 (1996)  
[self-destruction was triggered by an overflow error]
- North America blackout (2003)  
[race condition caused an alarm system failure]
- Mars Rover problems (2004)  
[interaction among concurrent tasks caused periodic sw resets]
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and pressed restart (even if you have a Mac)

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# Sequential Programming vs Concurrent Programming

## Sequential Programming

- Denotational semantics: the meaning of a program is a partial function from states to states
- Nontermination is bad!
- In case of termination, the result is unique

## Concurrent - Interactive - Reactive Programming

- Denotational semantics is very complicated due to nondeterminism
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# Analysis

Even short parallel programs may be hard to analyse, thus we need to face few questions:

- ① How can we develop (design) a system that “works”?
- ② How do we analyse (verify) such a system?

We need appropriate theories and **formal methods** and tools

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## Why formal methods?

- Understanding the overall behaviour resulting from system interactions can be tricky and error-prone

### Simple motivating example

Consider the code: `x = 1; y = x++ + x++;`

What is the value of `x` and `y` after its execution?

Consider the code: `g(x)=g(x-1)` with `f(x)=1;`

What is the value of `f(g(42))` after its execution?

- It is even more critical when concurrency and interactions enter the game. . .
- Solid mathematical foundations lay the basis for formal reasoning on systems behavior

The programmer can avoid operator `++`, but

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# Formal Methods for Reactive Systems

To deal with reactive systems and guarantee their correct behaviour in all possible environments, we need:

- 1 To study **mathematical models** for the formal description and analysis of concurrent programs
- 2 To devise **formal languages** for the specification of the possible behaviour of parallel and reactive systems

Each language comes equipped with **syntax & semantics**

- **Syntax**: defines legal programs (grammar based)
  - **Semantics**: defines meaning, behavior, errors (formally)
- 3 To develop **verification tools** and implementation techniques underlying them

# Process Algebraic Approach

- The chosen abstraction for reactive systems is the notion of **processes**: everything is (or can be viewed as) a process: buffers, shared memory, senders, receivers, ... are all processes
- Systems evolution is based on **process transformation**: a process performs an action and becomes another process
- A natural approach to the **design** of those systems structuring them into a set of components that can evolve independently and *communicate/synchronize*
  - **compositionality**: ability to build **complex distributed systems** by combining simpler systems
  - **abstraction**: ability to neglect certain parts of a model
- **Tools** assist modeling and analysis of the various functional and non-functional aspects of those systems
- Labelled Transition Systems (LTSs) describe processes behaviour, and permit modelling directly systems interaction

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# Internal and External Actions

## Labelled Transition Systems

**Transition Labelled Graph:** a transition between states is labelled by the action inducing the transition from one state to another

## Actions

An elementary action represents the *atomic* (non-interruptible) abstract step of a computation that is performed by a system

Actions represent various activities of concurrent systems:

- Sending a message
- Receiving a message
- Updating values
- Synchronizing with other processes . . .

We have two main types of atomic actions:

- Visible Actions
- Internal Actions ( $\tau$ )



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# Why operators for describing systems

How can we describe very large automata or LTSs?

As a table?

Rows and columns are labelled by states, entries are either empty or marked with a set of actions

As a listing of triples?

$\rightarrow = \{(q_0, a, q_1), (q_0, a, q_2), (q_1, b, q_3), (q_1, c, q_4), (q_2, \tau, q_3), (q_2, \tau, q_4)\}$

As a more compact listing of triples?

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# Why operators for describing systems

Linguistic aspects are important!

The previous solutions are ok for machines . . . not for humans

Are prefix and sum operators sufficient?

They are ok to describe small finite systems

- $p = a.b.(c+d)$
- $q = a.(b.c+b.d)$
- $r = a.b.c+a.c.d$

But additional operators are needed

- to design systems in a structured way (e.g.  $p \mid q$ )
- to model systems interaction
- to abstract from details
- to represent infinite systems



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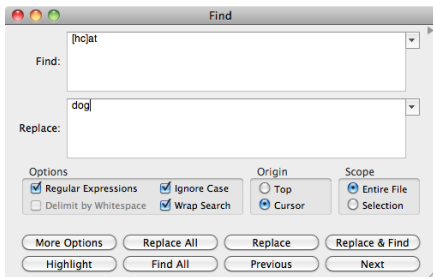
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# A motivating example: regular expressions

Commonly used for **searching and manipulating text based on patterns**



## Example

*Regular expression:* `[hc]at`  $\Rightarrow$   $(h + c); a; t$

*Text:* the cat eats the bat's hat rather than the rat

*Matches:* cat, hat

# A motivating example: regular expressions

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Commonly used for:

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  - representing regular languages in a compact form
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- Regular expressions as a simple programming language
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Before syntax and semantics. . .

. . . a few preliminaries