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Case-Based Reasoning

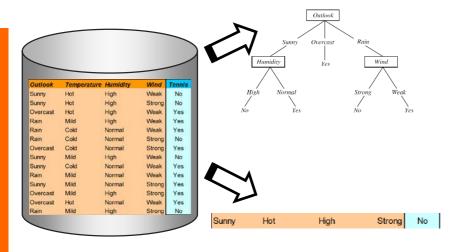
Knut Hinkelmann

Literature: Bergmann, Ralph: Experience Management. Springer-Verlag 2002





Two ways of Learning from Experience



There are two ways of learning from data

- Machine Learning:
 - Learn a set of rules from data
 - Apply this model for any new case
- ◆ Case-Based Reasoning (CBR):
 - For a new situation find the most similar data set and take the conclusion
 - If no appropriate data set is found, solve the new case ad hoc and store it



Humans Use Cases for Problem Solving

Examples:

- A medical doctor remembers the case history of another patient
- A lawyer argues with similar original precedence
- An architect studies the constrcution of existing building
- A work scheduler remembers the construction steps of a similar workpiece (Variant)
- A mathematician tries to transfers a known proof to a new problem
- A service technician remembers a similar defect at another device



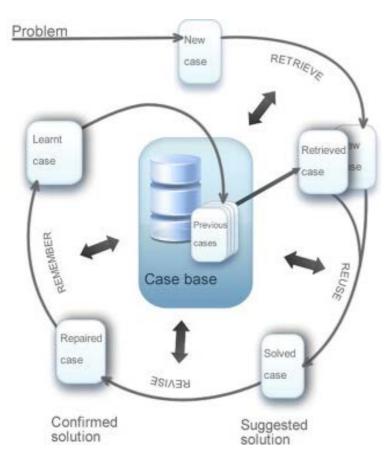
Machine Learning vs. Case Based Reasoning

- Machine Learning
 - ♦ can deliver good rules, if enough data sets are available
- Case-Based Reasoning
 - ♦ If not enough data sets are available
 - ♦ If there are many different or complex solutions



Case-Based Reasoning

Assumption: Similar problems have similar solutions



Source: A. Aamodt, E. Plaza (1994); AI Communications, IOS Press, Vol. 7: 1, pp. 39-59.

General approach:

- Experiences are stored as cases
- To solve a new problem ...
 - ... retrieve similar cases
 - ... solution of the most similar case is reused in the new situation
- If there is no similar case (or solution does not work) ...
 - ... derive a new solution
 - ... store it as a new case

Quelle: Bergmann

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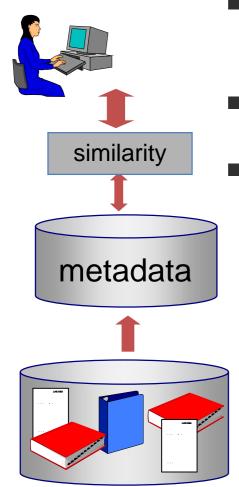




Application Example: Information Retrieval

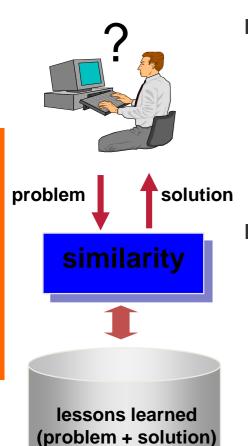


- Assume you look for the following car:
 - ♦ Audi A4, limousine, 125 PS, colour silver, automatic transmission, 2 years, bis 30'000 Fr.
- Problem: The database does not contain a car with exact this equipment
- Objective: The system should suggest those cars that are most similar to the one I look for, e.g..
 - ♦ Audi A4, limousine, 150 PS, blue, 5 gears, 2 years, €28.000
 - Audi A4, station waggon, 125 PS, silver, automatic transmission, 3 years, €26.000
 - ♦ BMW 320, limousine, 138 PS, silver, automatic transmission, 2 years, €29.500
 - Volvo S40, limousine, 125 PS, silver, automatic transmission, 18 months, €29.000
 - similarity = relaxing query





Learning from Experience: A simple Example (Overview)



Repairing a Car

- Symptoms are observed (e.g. engine doesn't start)
 and values are measured (e.g. battery voltage = 6.3V)
- ♦ Goal: Find the cause for the failure (e.g. battery empty) and a repair strategy (e.g. charge battery)

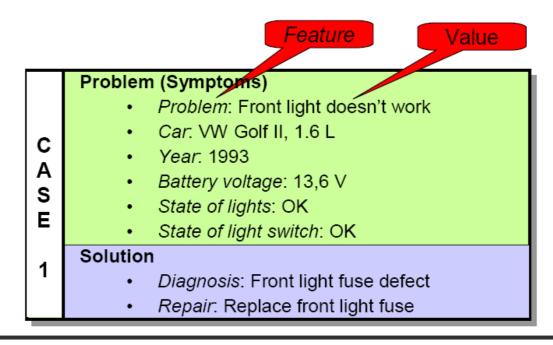
Case-Based Diagnosis:

- ♦ A case describes a diagnostic situation and contains:
 - description of the symptoms
 - description of the failure and the cause
 - description of a repair strategy
- ♦ A collection of cases is stored in a case base
- Find case similar to current problem and reuse repair strategy



A simple Example: What's in a Case

- A case describes one particular diagnostic situation
- A case records several features and their specific values
- Assumption: All cases are independent from each other



Source: Ralph Bergmann

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Example: A Case Base with 2 Cases

Problem (Symptoms)

Problem (Symptoms) Problem: Front light doesn't work Car: VW Golf II, 1.6 L Year: 1993 Battery voltage: 13,6 V State of lights: OK State of light switch: OK Solution Diagnosis: Front light fuse defect Repair: Replace front light fuse

Problem: Front light doesn't work Car: Audi A6 Year: 1995 Battery voltage: 12,9 V State of lights: surface damaged State of light switch: OK Solution



Source हिंदी कि निष्य विश्वनिष्य nann

Prof. Dr. Knut Hinkelmann Case-Based Reasoning

Diagnosis: Bulb defect

Repair: Replace front light



Solving a new Diagnostic Problem

- When a new problem occures, we make several observations in the current situation
 - Observations define a new problem
 - Not all feature values may be known
- Note: The new problem is a case without solution part

Problem (Symptom): • Problem: Break light doesn't work • Car: Audi 80 • Year: 1989 • Battery voltage: 12.6 V • State of light: OK

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Source: Ralph Bergmann



Compare the New Problem with Each Case and Select the Most Similar Case



Similarity is the most important concept in CBR !!

- When are two cases similar?
- How to rank the cases according to their similarity?
- We can assess similarity based on the similarity of each feature
 - ♦ Similarity of each feature depends on the feature value.



Source: Ralph Bergmann

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Similarity Computation

Assignment of similarities for features values. Not similar Very similar



- Express degree of similarity by a real number between 0 and 1 Examples:
 - Feature: Problem

Feature: Battery voltage (similarity depends on the difference)

$$12.6 \text{ V} \xrightarrow{0.9} 13.6 \text{ V}$$
 $12.6 \text{ V} \xrightarrow{0.1} 6.7 \text{ V}$

Different features have different importance (weights)!

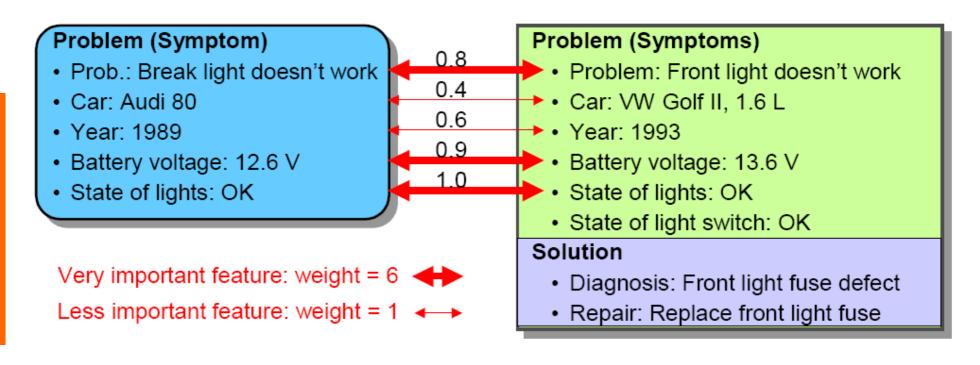


- High importance: Problem, Battery voltage, State of light, ...
- Low importance: Car, Year, ...

Source: Ralph Bergmann Prof. Dr. Knut Hinkelmann 12 Case-Based Reasoning



Compare New Problem and Case 1



Similarity Computation by Weighted Average

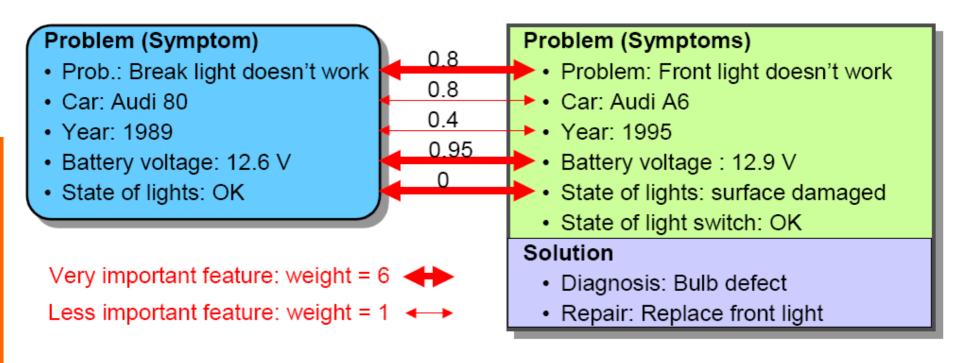
 $similarity(new, case 1) = \frac{1}{20} * [6*0.8 + 1*0.4 + 1*0.6 + 6*0.9 + 6*1.0] =$ **0.86**



Source: Ralph Bergmann



Compare New Problem and Case 2



Similarity Computation by Weighted Average

 $similarity(new, case 2) = \frac{1}{20} * [6*0.8 + 1*0.8 + 1*0.4 + 6*0.95 + 6*0] =$ **0.585**

Case 1 is more similar: due to feature "State of lights"

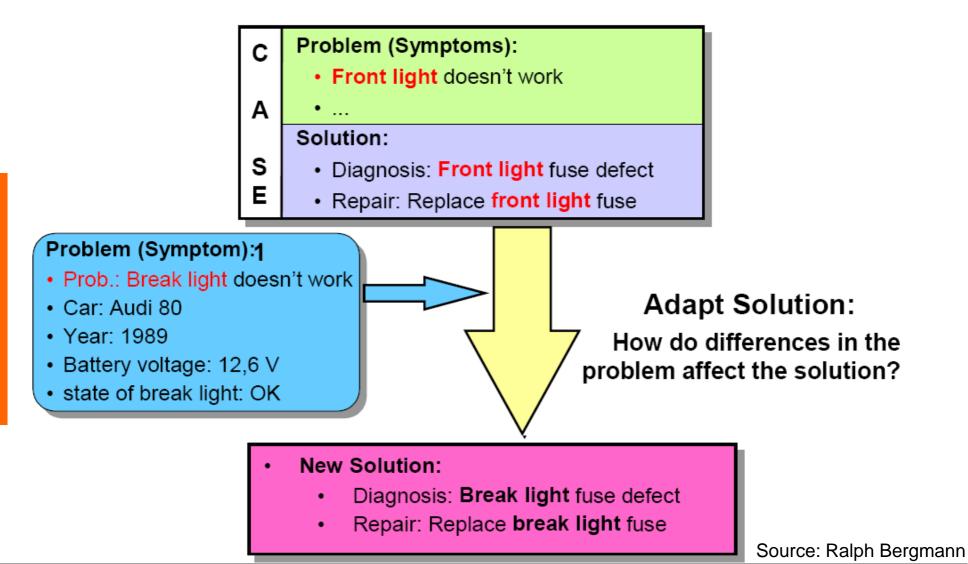


Source: Ralph Bergmann

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Reuse Solution of Case 1







Store the New Experience

If diagnosis is correct: store new case in the memory.

Problem (Symptoms):

C A

SE

3

Problem: Break light doesn't work

Car: Audi 80

Year: 1989

Battery voltage: 12.6 V

State of break lights: OK

light switch clicking: OK

Solution:

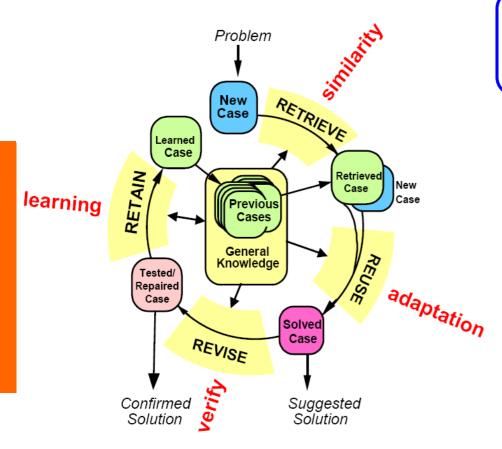
- Diagnosis: break light fuse defect
- Repair: replace break light fuse



Source: Ralph Bergmann



CBR Cycle



Retrieve ...

most similar case or cases

Reuse ...

the information and knowledge in that case to solve the problem

Revise ...

the proposed solution if necessary

Retain ...

the parts of this experience likely to be useful for future problem solving

Source: K.-D. Althoff & A. Aamodt: Relating case-based problem solving and learning methods to task and domain characteristics. Al Communications 1996



Prof. Dr. Knut Hinkelmann



Case Representation

Textual Approach

Frequently Asked Question 241

Title: Order numbers of CPUs with which communications is possible.

Question: Which order numbers must the S7-CPUs have to be able to run basic communications with SFCs?

Answer: In order to participate in communications via SFCs without a configured connection table, the module concerned must have the correct order number. The following table illustrates which order number your CPU must have to be able to participate in these S7 homogeneous communications.

Conversational Approach

Case: 241

Title: Printer does not work in the new release.

Q1: What kind of problem do you have? Printer Problem

Q1: Does the printer perform a self-test? Yes

Q2: Does the printer work with other software? Yes

Q3: Did you just install the software? Yes

Q4: Did you create a printer definition file? Yes

Q5: What release did you install? 4.2

Problem: Installation procedure overrides printer definition

Action: Reinstall the printer from disk 2.3

Structural Approach

Reference: AD8009

Price: 2.25

Input offset voltage: 2 mV Input bias current: 50 uA

Output voltage: 1.2 V

Output current drive: 175 mA

Single supply: No

PSPS: 70 dB

Number of devices per package : single

Available Package(s) : SOIC

(Bergmann 2002, p. 54ff)





Structural Cases: Attribute Value Representation

 A common approach for structural case representations are attribute value pairs



- As in programming language, types define allowed values for attributes. Examples of types are
 - numbers types like integer, real or intervals
 - symbols defined by
 - enumaration of symbols {red, yellow, green}
 - elements of a knowledge structure, e.g. classification scheme
 - text such as strings or markups
 - special types like URLs



(Bergmann 2002, p. 62)

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Example: Searching for Used Car

car 1:

model: Audi A4

♦ year: 2012

price: 15'000

type: station waggon

transmission: automatic

extra: AC

car 2:

model: Audi A3

year: 2013

• price: 20'000

type: limousine

transmission: 5 gear

extra: CD, handsfree-kit

query:

model: VW Golf

♦ year: 2014

price: 18'000

type: station waggon

transmission: 4 gear

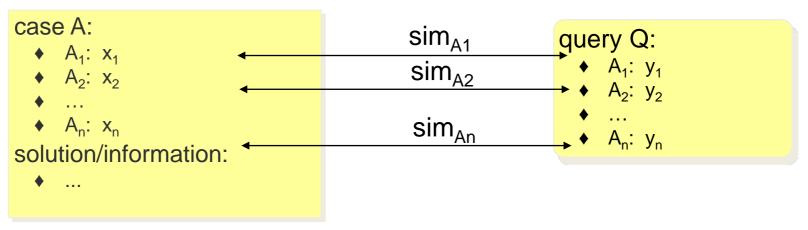
extra: AC, handsfree-kit



Similarity Calculation for Attribute-Value Pairs

Cases resp. meta-data are represented by *n* attributes A₁,...,A_n

each attribute A_i has type T_i



Local similarity: for each attribute a similarity function is defined

- \bullet sim_{Ai} (x_i,y_i): T_i x T_i \rightarrow [0..1]
- local similarity measures depend on the type of the attribute

Global similarity: combining values for local similarity

- \bullet sim(A,Q) = F(sim_{A1}(x₁,y₁), sim_{A2}(x₁,y₁), ..., sim_{An}(x_n,y_n))
- ♦ F:[0..1]n → [0..1] is called an **aggregation function**





Similarity Measure

Definition: A *similarity measure* is a function sim: M x M \rightarrow [0,1]

- This definition restricts similarity to a number in the intervall [0,1].
 - ♦ It allows to express the most similar (1) und the least similar (0) situation
 - ♦ It also allows to express degrees of similarity: if sim(x,y) > sim(x,z), then x is more similar to y than to z

%

(Bergmann 2002, p. 96)



CBR vs. Database Query

- Remark: Query answering in SQL can be seen as a special case of a similarity measure where the value range is a set {0,1}
 - \bullet sim(x,y) = 1 (equal) or
 - \bullet sim(x,y) = 0 (unequal)

Database System	CBR System
 simple search ⇒ "all or nothing" 	using same database but search for most similar cases
often too many hits (underspecification) or no hits at all (overspecification)	system can be told to show only, e.g., 10 cases by descending order
no specific domain knowledge used for the search	considers domain knowledge for search by using similarity measures, e.g., spatial or geographical relations
pure database applications cannot be used for online consulting	online consulting is the power of a CBR system

(Bergmann 2002, p. 96)





Usual Properties for Similarity Measures

■ A similarity measure is called *reflexive* if

$$sim(x,x) = 1$$

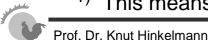
holds for all x^{-1}

- If additionally sim(x,y) = 1 implies that x = y, then the similarity measure is called *strong reflexive*
- A similarity measure is called *symmetric* if for all x,y it holds that sim(x,y) = sim(y,x)

Symmetric: it is not important for the similarity computation which attribute value belongs to the query and which one belongs to the case

Assymetric: it is important which value belongs to the query and which one belongs to the case; a major example is the attribute *price*.

(Bergmann 2002, p. 101f)



¹⁾ This means that for every value x of M, x is maximally similar to itself

mann Case-Based Reasoning 24



Meanings of Similarity.

Similarity ...

- ... always refers to a specific aspect
 - ♦ Example: Two cars are similar if they
 - are of the same brand
 - have similar maximum speed
- ... is not necessarily transitive
 - ♦ Example: For integers we can say that
 - 2 is similar to 4
 - 4 is similar to 6
 - ...
 - 99998 is similar to 100.000

But: Is 2 similar to 100.000?

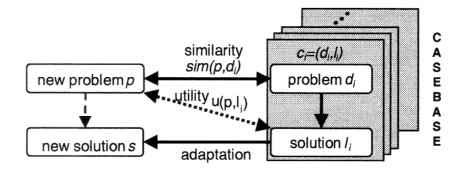
- ... is not necessarily symmetric
 - ♦ if I look for a limousine, I probably could accept a station wagon
 - if I need a station wagon because of the space, a limousine might less acceptable for me





Approximating Utility with Similarity

- Assumption
 - Similar problems have similar solutions
 - ♦ The solution of a problem is also useful for similar problems
- Utility of a case c for a problem p is approximated by the similarity between the problem p and problem d contained in case c



Remark:

- Utility is an a posteriori criteria: It can be assessed after after the problem was solved.
- ♦ Similarity is an a priori criteria: It must be assessed before problem solving.
- Utility corresponds to relevance in information retrieval



(Bergmann 2002, p. 94)



Local Similarity Measure for Numeric Attributes

For numeric attributes, similarity is computed as a function of distance d:

$$sim_A(x,y) = f(|d(x,y)|)$$

- Typical distance functions are the following two:
 - standard linear distance (= difference) d(x,y) = |x y|
 - ♦ logarithmic distance $d(x,y) = |\log(x) \log(y)|$

(logarithmic distance is used for exponentially scaled value ranges. i.e. if the value range for the attribute spans several orders of magnitude)

Examples of similarity measure for numeric attributes:

linear function

$$sim_A(x,y) = 1 - \frac{|x-y|}{max(|x-y|)}$$

non-linear function

$$sim_A(x,y) = \frac{1}{1 + (|x-y|)}$$



(Bergmann 2002, p. 107)



Local Similarity Measure for Numeric Attributes

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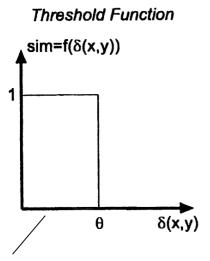
non-linear function

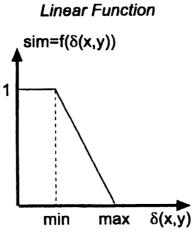


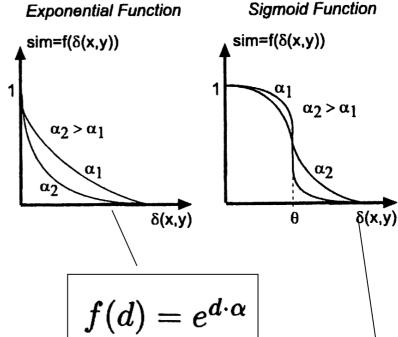
(Bergmann 2002, p. 107)



Further Functions for Numeric Similarity Measures







$$f(d) = \begin{cases} 1 : & d < \theta \\ 0 : & d \ge \theta \end{cases}$$

$$f(d) = \begin{cases} 1 & : d < min \\ \frac{max - d}{max - min} & : min \le d \le max \\ 0 & : d > max \end{cases}$$

$$f(d) = rac{1}{e^{rac{d- heta}{lpha}}+1}$$

(Bergmann 2002, p. 108f)





Symmetry for Numeric Values

Symmetric:

- it is not important for the similarity computation which attribute value belongs to the query and which one belongs to the case
- ♦ Example: for numeric values use the absolute distance d = |query value case value|
 - sim(x.y) = f(d(x,y))

Asymmetric:

- ♦ it is important which value belongs to the query and which one belongs to the case; a major example is the attribute *price*.
- similarity can be computed with two different similarity functions

$$sim(x,y) = \begin{cases} f_1(d(x,y)) & \text{if } x>y\\ 1 & \text{if } x=y\\ f_2(d(x,y)) & \text{if } x$$





Local Similarity for Ordered Symbols

- For symbolic attributes we can distinguish approaches depending on whether there is an order defined on the symbols or not.
- Example for ordered symbols: qualitative values, e.g. {small, medium, large}
 - ♦ small < medium < large</p>
- With such an order defined, we can determine the similarity by using the ordinal number of the symbols, e.g.
 - ♦ small --> 1
 - ♦ medium --> 2
 - ♦ large --> 3

and applying similarity measure for numeric attributes



Local Similarity for unordered Symbols

If there is no obvious ordering on the set of attribute values and no odering can be defined, we can apply the tabular approach

 \bullet sim_A(x,y) = s[x,y]

cases y

query x

s[x,y]	limousine	convertible	station
limousine	1	0.3	0.7
convertible	0.4	1	0.2
station	0.5	0.2	1

similarity of x and y

- Reflexive similarity measure: diagonal values are 1
- Symmetric similarity measure:
 upper triangular matrix = lower triangular matrix

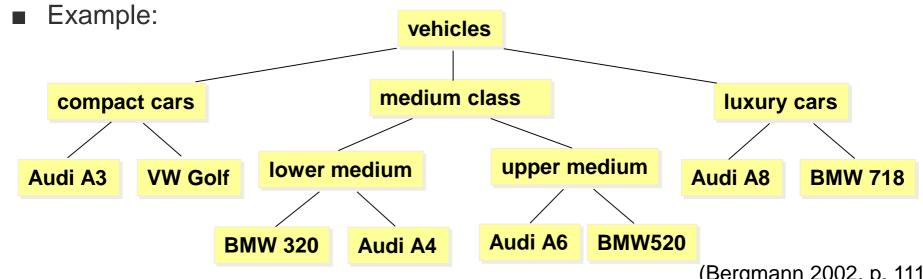


<u>cp. (Bergmann 2002, p. 110)</u>



Taxonomically Ordered Symbolic Types

- A special variant of symbolic types are taxonomies. A taxonomy is a tree in which the nodes represent symbolic values
- A taxonomy represents an additional releationship between the symbols
 - Leaf nodes represent concrete objects of the real world
 - Inner nodes represent classes of real world objects.
 - An inner node k stands for the set of real world objects represented by leaf nodes below it

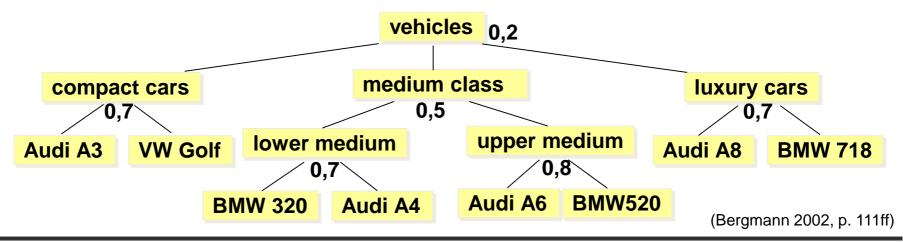






Similarity Measure for Taxonomies

- Inner nodes cluster real-world objects that have some properties in common.
- The deeper we decent in the taxonomy, the more features do the objects have in common
- Similarity measures in a taxonomy
 - ♦ Every inner node K_i is annotated with a similarity value S_i
 - The deeper the nodes in the hierarchy, the larger the similarity value can become
 - Meaning: All elements belonging to a class have the similarity measure assigned to the class





Computing Similarity Measure between Leaf Nodes of a Taxonomy

- Leaf nodes represent concrete element objects
- Similarity of two leaf nodes is the similarity value of the lowest

common predecessor

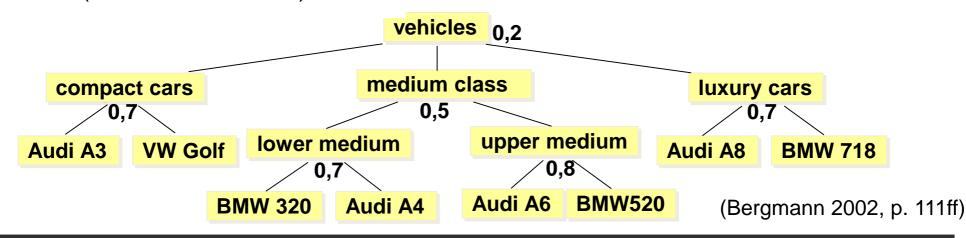
 $sim(K_1, K_2) = \begin{cases} 1 : K_1 = K_2 \\ S_{\langle K_1, K_2 \rangle} : K_1 \neq K_2 \end{cases}$

Example:

sim(BMW320, AudiA4) =

sim(BMW320, AudiA6) =

sim(BMW320, AudiA8) =





Semantics and Similarity of Inner Nodes

An inner node can have different meanings

- Any value in the query: The inner node in the query stands for any value below this node.
 - Example: A person is looking for a compact car but does not care whether it is an Audi A3 or a VW Golf
 - Sample query: "compact car"
- Any value in the Case: Typically cases have concrete values, but it could also include inner nodes, which stand for any value below the node
 - ♦ Assume a car dealer specifies that he sells any compact cars
- Uncertainty: The use of an inner node K means that we do not know the exact value for this attribute, but we know that it must be a concrete value below this node
 - ♦ Assume a car dealer specifies that he sells a single compact car without saying whether it is a Audi A3 or a VW Golf



(Bergmann 2002, p. 111ff)



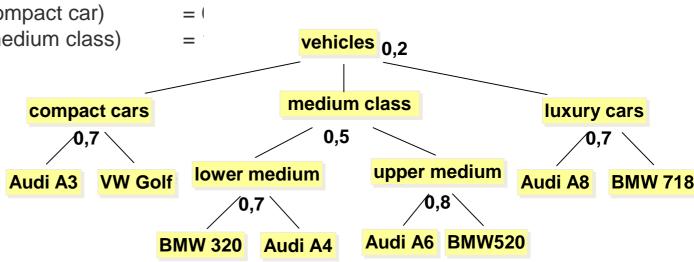
Similarity with inner Nodes of a Taxonomy: Any Value (1/2)

We are looking for the highest possible similarity sim(Q,C) 1)

- ♦ sim(compact car, AudiA3)
- sim(medium class, AudiA4) =
- sim(medium class, AudiA3) = 0

Also possible for an inner node in a case:

- ♦ sim(AudiA4, medium class) =
- ♦ sim(AudiA3, medium class) = 0
- sim(medium class, compact car) = 0
- sim(lower medium, medium class)



1) The first parameter of sim(Q.C) is the query, the second parameter is the case description





Similarity with inner Nodes of a Taxonomy: Any Values (2/2)

- Inner node in the query or in the case
 - ♦ All leaf nodes below the inner node have similarity 1
 - ◆ For all other nodes: Take the similarity of the lowest common predecessor.

$$sim_{A_i}(Q,C) = \max\{sim(q,c)|q \in L_Q, c \in L_C\}$$

$$= \begin{cases} 1 & : & C < Q \text{ or } Q < C \\ S_{\langle Q,C \rangle} & : & \text{otherwise} \end{cases}$$

Notation:

Q Query

C Case

L_Q, L_C leaf nodes below Q or C

C < Q C is below Q in the taxonomy

(Q is predecessor of C)

 $S_{\text{< Q.C>}}$ similarity of the lowest common predecessor of Q and C



(Bergmann 2002, p. 118)



Multiple Attribute Values

- Attributes can contain multiple values
 - $A_{query} = \{a_1, ..., a_n\}$
 - $A_{case} = \{b_1, ..., b_m\}$
- Similarity measure for sets:
 - ◆ Compute all pairs of similarity measures sim_A(a_i,b_i)
 - ◆ Aggregate the local similarity sim_A(A_{query}, A_{case})

=
$$MF(sim_A(a_1,b_1),...,sim_A(a_1,b_m),...,sim_A(a_n,b_1),...,sim_A(a_n,b_m))$$

- There are various possible approaches for the aggregate function MF, e.g.
 - minimum
 - maximum
 - average





Unknown Attribut Values

- It often occurs that attribute values are not known (NULL):
- Strategies to deal with unknown values
 - optimistic strategy: Assume that unknown values are most similar: sim(NULL,x) = 1
 - ♦ pessimistic strategy: Assume that unknown values are least similar: sim(NULL,x) = 0.
 - strategy of expected value: Use an expected value, e.g. based on probability or average
 - ignore the attributes



Global Similarity

- Global similary measures are defined by applying an aggregation function F : [0..1]ⁿ → [0..1] to the local similarity values.
 - ♦ Input: Local similarity measures sim_{Ai}(x_i, y_i) for each attribute A_i
 - ♦ Global similarity:

$$sim(x,y) = F (sim_{A1}(x_1, y_1), ..., sim_{An}(x_n, y_n))$$

- Possible properties for F
 - F is monotone in each argument
 - F(0,...,0) = 0
 - F(1,...,1) = 1





Basic Aggregation Functions

■ Weighted Average:
$$F(s_1,...,s_n) = \sum_{i=1}^{n} w_i \cdot s_i$$

with
$$\sum_{i=1}^{n} w_i = 1$$

■ Generalized weighted average: $F(s_1,...,s_n) = \frac{\alpha}{\sqrt{\sum_{i=1}^n w_i \cdot s_i^{\alpha}}}$

with
$$\alpha \in \mathbb{R}^+$$
 und

$$\sum_{i=1}^{n} w_i = 1$$

$$F(s_1,...,s_n) = \max_{i=1}^{n} \max(w_i \cdot s_i)$$

$$F(s_1,...,s_n) = \min_{i=1}^n \min(w_i \cdot s_i)$$



<u>(Bergmann 2002, p. 120f</u>

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