

Andrea Polini

Process Mining MSc in Computer Science (LM-18) University of Camerino





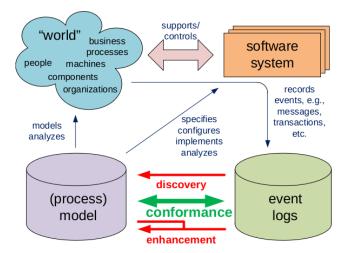












Motivations

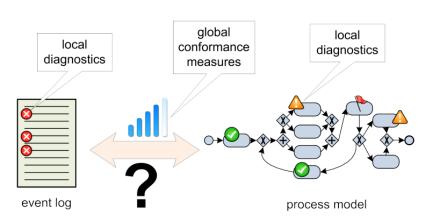


Why?

Conformance checking relates events in the event log to activities in the process model and compares both. The goal is to find commonalities and discrepancies between the modeled behavior and the observed behavior. Conformance checking is relevant for business alignment and auditing:

- ► find undesirable deviations suggesting fraud or inefficiencies
- measuring the performance of process discovery algorithms
- repair models that are not aligned well with reality

Using Conformance Checking



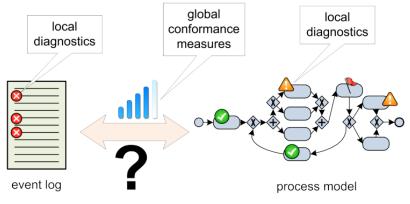
- global conformance measures e.g. 85% of the cases in the event log can be replayed by the model
- local diagnostics e.g. activity x was executed 15 times although this was not allowed according to the model

Results Interpretation



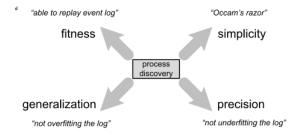
The interpretation of non-conformance depends on the purpose of the model:

- descriptive
- normative



Quality criteria



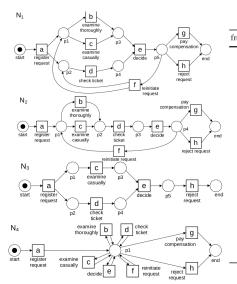


Fitness function

- A naïve approach towards conformance checking would be to simply count the fraction of cases that can be "parsed completely"
 - $\blacktriangleright N_1 : 1, N_2 : 0.6815, N_3 : 0.4543, N_4 : 1$

Four models and one log





requency	reference	e trace
455	σ_1	$\langle a, c, d, e, h \rangle$
191	σ_2	$\langle a, b, d, e, g \rangle$
177	σ_3	$\langle a, d, c, e, h \rangle$
144	σ_4	$\langle a, b, d, e, h \rangle$
111	σ_5	$\langle a, c, d, e, g \rangle$
82	σ_6	$\langle a, d, c, e, g \rangle$
56	σ_7	$\langle a, d, b, e, h \rangle$
47	σ_8	$\langle a, c, d, e, f, d, b, e, h \rangle$
38	σ_9	$\langle a, d, b, e, g \rangle$
33	σ_{10}	$\langle a, c, d, e, f, b, d, e, h \rangle$
14	σ_{11}	$\langle a, c, d, e, f, b, d, e, g \rangle$
11	σ_{12}	$\langle a, c, d, e, f, d, b, e, g \rangle$
9	σ_{13}	$\langle a, d, c, e, f, c, d, e, h \rangle$
8	σ_{14}	$\langle a, d, c, e, f, d, b, e, h \rangle$
5	σ_{15}	$\langle a, d, c, e, f, b, d, e, g \rangle$
3	σ_{16}	$\langle a, c, d, e, f, b, d, e, f, d, b, e, g \rangle$
2	σ_{17}	$\langle a, d, c, e, f, d, b, e, g \rangle$
2	σ_{18}	$\langle a, d, c, e, f, b, d, e, f, b, d, e, g \rangle$
1	σ_{19}	$\langle a, d, c, e, f, d, b, e, f, b, d, e, h \rangle$
1	σ_{20}	$\langle a, d, b, e, f, b, d, e, f, d, b, e, g \rangle$
1	σ_{21}	$\langle a,d,c,e,f,d,b,e,f,c,d,e,f,d,b,e,g \rangle$

Token Based Metrics



- The fitness metric is generally defined at the level of events
 - Let's continue to replay a trace adding (and counting) tokens to enable blocked transitions, and also counting the remaining tokens at the end of the execution

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Let's consider model N_1 , the following four counters,

- p: number of produced tokens
- c: number of consumed tokens
- m: number of added tokes
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Now let's replay the trace on N_2



$$fitness(\sigma, N) = \frac{1}{2} \left(1 - \frac{m}{c} \right) + \frac{1}{2} \left(1 - \frac{r}{p} \right)$$

- What about replaying trace $\sigma_2 = \langle a, b, d, e, g \rangle$ on N_3 ?
- When a trace contains labels for which there is no corresponding transition the trace has to be projected on the available transitions

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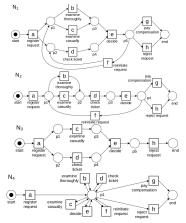
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$$\sigma_2 = \langle \boldsymbol{a}, \boldsymbol{b}, \boldsymbol{d}, \boldsymbol{e}, \boldsymbol{g} \rangle \rightarrow \sigma_2' = \langle \boldsymbol{a}, \boldsymbol{d}, \boldsymbol{e} \rangle$$

Computing fitness at the log level



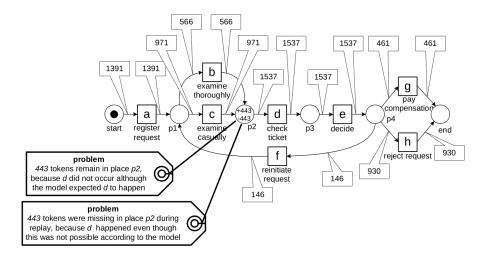
$$\textit{fitness}(L, N) = \frac{1}{2} \left(1 - \frac{\Sigma_{\sigma \in L} L(\sigma) \times m_{N,\sigma}}{\Sigma_{\sigma \in L} L(\sigma) \times c_{N,\sigma}} \right) + \frac{1}{2} \left(1 - \frac{\Sigma_{\sigma \in L} L(\sigma) \times r_{N,\sigma}}{\Sigma_{\sigma \in L} L(\sigma) \times p_{N,\sigma}} \right)$$



- fitness $(L_{full}, N_1) = 1$
- fitness $(L_{full}, N_2) = 0.9504$
- $fitness(L_{full}, N_3) = 0.8797$
- fitness $(L_{full}, N_4) = 1$

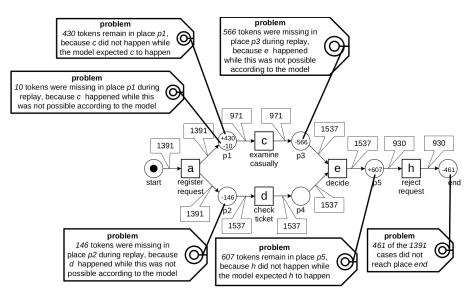
Diagnostics (N_2)





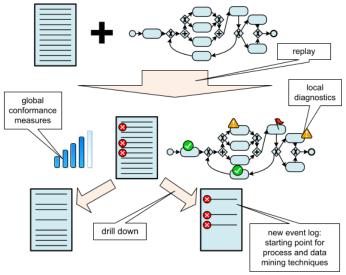
Diagnostics (N₃)





Further analysis







Using token-based replay we can differentiate between fitting and non-fitting cases

Drawbacks

- Fitness values tend to be too high for extremely problematic event logs
- If there are many deviations, the Petri net gets "flooded with tokens" and subsequently allows for any behavior
- The approach is also Petri-net specific and can only be applied to other representations after conversion
- If a case does not fit, the approach does not create a corresponding path through the model.

Alignments were introduced to overcome these limitations



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Alignments were introduced to overcome these limitations

A so-called optimal alignment is a best match given a trace and a model. Given $\sigma = \langle a, d, b, e, h \rangle$ and N_1 there is precisely one optimal alignment

$$\gamma_{2a} = \left| \begin{array}{c|c|c} a & d & b & e & h \\ \hline a & d & b & e & h \\ \end{array} \right|$$

Given σ and N_2 there are multiple optimal alignments:

$$\gamma_{2a} = \frac{\begin{vmatrix} a \\ a \end{vmatrix} > \begin{vmatrix} d \\ b \end{vmatrix} > \begin{vmatrix} e \\ b \end{vmatrix}} > \begin{vmatrix} e \\ b \end{vmatrix}} > \frac{\begin{vmatrix} a \\ b \end{vmatrix} > \begin{vmatrix} e \\ c \end{vmatrix}} > \frac{\begin{vmatrix} a \\ c \end{vmatrix}} > \frac{\begin{vmatrix} a \\ c \end{vmatrix} > \begin{vmatrix} e \\ c \end{vmatrix}} > \frac{\begin{vmatrix} a \\ c$$





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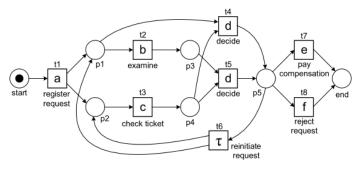
Given σ and N_2 there are multiple optimal alignments:

$$\gamma_{2a} = \begin{vmatrix} a & \gg & d & b & e & h \\ \hline a & b & d & \gg & e & h \\ \hline \end{pmatrix} \qquad \gamma_{2b} = \begin{vmatrix} a & \gg & d & b & e & h \\ \hline a & c & d & \gg & e & h \\ \hline \end{pmatrix}$$
$$\gamma_{2c} = \begin{vmatrix} a & d & b & \gg & e & h \\ \hline a & \gg & b & d & e & h \\ \hline \end{pmatrix}$$

Token-based conformance checking becomes more complicated when there are duplicate and silent activities, e.g., transitions with a τ label or two transitions with the same label. Alignments can be defined for any process notation having duplicate and silent activities

Silent and duplicated transition (N5)





 $\sigma = \langle \textit{a},\textit{c},\textit{d},\textit{b},\textit{c},\textit{d},\textit{c},\textit{d},\textit{c},\textit{b},\textit{d},\textit{f} \rangle$

Which is the corresponding alignment?

Move and Alignments



Move

A move is a pair (x, (y, t)) where the first element refers to the log and the second element refers to the model.

(x, (y, t)) is a legal move if one of the following four cases holds:

- x = y and y is the visible label of transition t (synchronous move)
- $x = \gg$ and y is the visible label of transition t (visible model move)
- $x = \gg$, $y = \tau$ and transition t is silent (invisible model move)
- $x \neq \gg$ and $(y, t) = \gg$ (log move)

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Alignment

An alignment is a sequence of legal moves such that after removing all \gg symbols, the top row corresponds to the trace in the log, and the bottom row corresponds to a firing sequence starting in some initial state of the process model and ending in some final state.

Selecting alignments



Given a log trace and a process model, there may be many (if not infinitely many) alignments. For $\sigma_2 = \langle a, b, d, f \rangle$ and N_5 , there are additional alignments like:

<u></u>	a	b	$ \gg $	d	f			а	b	d	f	\gg	\gg	\gg	\gg	\gg	
$\gamma_{\rm 5,2a} =$	а	b	С	d	f) 75	,2c =	\gg	\gg	\gg	\gg	а	b	С	d	f	
	t ₁	t ₂	t ₃	t ₅	t ₈							<i>t</i> ₁	t ₂	t ₃	t ₅	t ₈	
0 /		a	\gg	b	d	f			а	b	d	f	\gg	\gg	\gg		
$\gamma_{5,2}$	b —	a	С	b	d	f	$\gamma_{5,2}$	d —	а	\gg	\gg	\gg	С	d	е		
		t ₁	t ₃	t ₂	<i>t</i> 5	t ₈			t ₁				t ₃	<i>t</i> 4	t7		

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$\gamma_{\rm 5,2a} =$	а	b	С	d	f) 75	,2c =	\gg	\gg	\gg	\gg	а	b	С	d	f	
	t ₁	t ₂	t ₃	t ₅	t ₈							t ₁	t ₂	t ₃	t ₅	t ₈	
a /= -		а	\gg	b	d	f	a /		а	b	d	f	\gg	\gg	\gg		
$\gamma_{5,2}$	b —	а	С	b	d	f	$\gamma_{5,2}$	d —	а	\gg	\gg	\gg	С	d	е		
		t ₁	t ₃	t ₂	t ₅	t ₈			t ₁				t ₃	t ₄	t7		

To select the most appropriate alignment, we associate costs to undesirable moves and select an alignment with the lowest total costs. Cost function δ as- signs costs to legal moves.

- Moves where log and model agree have no costs, i.e., $\delta(x, (y, t)) = 0$ for synchronous moves (with x = y)
- Moves in model only have no costs if the transition is invisible, i.e., $\delta(\gg, (\tau, t)) = 0$ for invisible model moves
- δ(≫, (y, t)) > 0 is the cost when the model makes an "y move" without a corresponding move of the log (visible model move)
- δ(x, ≫) > 0 is the cost for an "x move" in just the log (log move)

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o/ —	a	b	≫	d	f				b	d	f	\gg	\gg	\gg	\gg	\gg
$\gamma_{\rm 5,2a} =$	a	b	С	d	f) '/5	$\gamma_{5,2c} = $	\gg	\gg	\gg	\gg	а	b	С	d	f
	t ₁	t ₂	t ₃	t ₅	t ₈							t ₁	t ₂	t ₃	<i>t</i> 5	t ₈
- '		a	\gg	b	d	f	0/	. —	а	b	d	f	\gg	>>	>>	
$\gamma_{5,2}$	b —	а	С	b	d	f	f ^{75,2}		а	\gg	\gg	\gg	С	d	е	
		<i>t</i> ₁	t ₃	t ₂	t ₅	t ₈			t ₁				t ₃	t ₄	t7	

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An alignment is optimal if there is no alternative alignment with lower costs

Fitness



$$\textit{fitness}(\sigma, \textit{N}) = 1 - \frac{\delta(\lambda_{\textit{opt}}^{\textit{N}}(\sigma))}{\delta(\lambda_{\textit{worst}}^{\textit{N}}(\sigma))}$$

where:

- $\delta(\lambda_{opt}^{N}(\sigma))$: cost for the optimal alignment
- δ(λ^N_{worst}(σ)): cost for the worst alignment (log moves and shortest path from the initial state to a final state)

Fitness



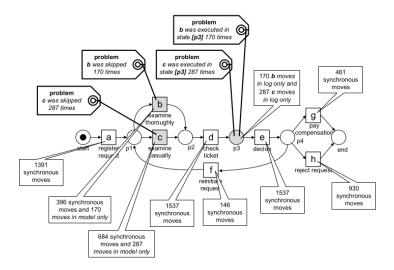
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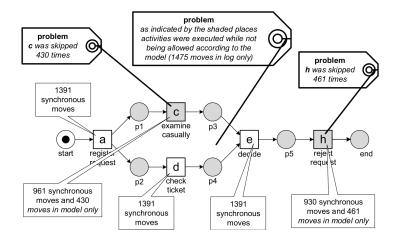
- $\delta(\lambda_{opt}^{N}(\sigma))$: cost for the optimal alignment
- δ(λ^N_{worst}(σ)): cost for the worst alignment (log moves and shortest path from the initial state to a final state)

$$\textit{fitness}(L, N) = 1 - \frac{\sum_{\sigma \in L} L(\sigma) \times \delta(\lambda_{opt}^{N}(\sigma))}{\sum_{\sigma \in L} L(\sigma) \times \delta(\lambda_{worst}^{N}(\sigma))}$$











The following differences exist between token-based and alignment-based conformance checking:

- Alignments provide more detailed but easy to understand diagnostics. Skipped and inserted events are easier to interpret than missing and remaining tokens.
- Alignments provide more accurate diagnostics. Token-based replay may provide misleading diagnostics due to remaining tokens (earlier deviations mask later deviations). As a result fitness values are generally too low
- Alignments are configurable through the cost function. One can use multiple cost functions depending on the likelihood of a deviation and its severity.
- Alignments can be used to map each case onto a feasible path in model. This is important for projecting information (e.g., bottlenecks) on models. Moreover, the mapping ensures that non-fitting extra behavior is not causing misleading diagnostics. Token-based replay also relates observed and modeled behavior, but does not create the corresponding end-to-end execution sequences in the model.
- Alignments are model independent. Any process model with formal semantics and initial and final states can be used. Token-based replay assumes a Petri net, so conversions may be needed (e.g., from BPMN to Petri nets).
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Comparing footprints



	а	b	С	d	е	f	g	h
а	#	\rightarrow	\rightarrow	\rightarrow	#	#	#	#
b	\leftarrow	#	#		\rightarrow	\leftarrow	#	#
С	\leftarrow	#	#		\rightarrow	\leftarrow	#	#
d	\leftarrow			#	\rightarrow	\leftarrow	#	#
е	#	\leftarrow	\leftarrow	\leftarrow	#	\rightarrow	\rightarrow	\rightarrow
f	#	\rightarrow	\rightarrow	\rightarrow	\leftarrow	#	#	#
g	#	#	#	#	\leftarrow	#	#	#
h	#	#	#	#	\leftarrow	#	#	#

Footprint for L_{full} and N_1

Comparing footprints



	а	b	С	d	е	f	g	h
а	#	\rightarrow	\rightarrow	#	#	#	#	#
b	\leftarrow	#	#	\rightarrow	#	\leftarrow	#	#
с	\leftarrow	#	#	\rightarrow	#	\leftarrow	#	#
d	#	\leftarrow	\leftarrow	#	\rightarrow	#	#	#
е	#	#	#	\leftarrow	#	\rightarrow	\rightarrow	\rightarrow
f	#	\rightarrow	\rightarrow	#	\leftarrow	#	#	#
8	#	#	#	#	\leftarrow	#	#	#
h	#	#	#	#	\leftarrow	#	#	#

Footprint for N_2

Comparing footprints



	а	b	С	d	е	f	g	h
а				→: #				
b				$\ :\rightarrow$	\rightarrow :#			
с				$\ :\rightarrow$	\rightarrow :#			
d	←:#	:←	:←			←:#		
е		←:#	←:#					
f				\rightarrow :#				
g								
h								

Differences between footprint L_{full} ed N₂

Additional usage of conformance checking



- Repairing models
- Evaluating Process Discovery Algorithms
- Connecting event log and process model